

Many-Body Effects in the Magnetization Tunneling of an Ensemble of Mesoscopic Spins

highly diluted Ho³⁺ ions in LiYF₄

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Outline

➤ *Introduction*

➤ *The quantum dynamics of a single Ho^{3+} ion*

- ✓ Origin of the mesoscopic behavior
- ✓ Strong hyperfine coupling limit
- ✓ Hysteresis loops @ low field sweep rates

➤ *The quantum dynamics of an ensemble of Ho^{3+} ions*

- ✓ Cross-spin relaxations (co-tunneling & biased tunneling)
- ✓ Anisotropic interactions
- ✓ Hysteresis loops @ fast field sweep rates; Ac-susceptibility

➤ *Conclusion*

About the large scale ...

➤ Mesoscopic spins ($S \sim 10$) periodic 3D-array

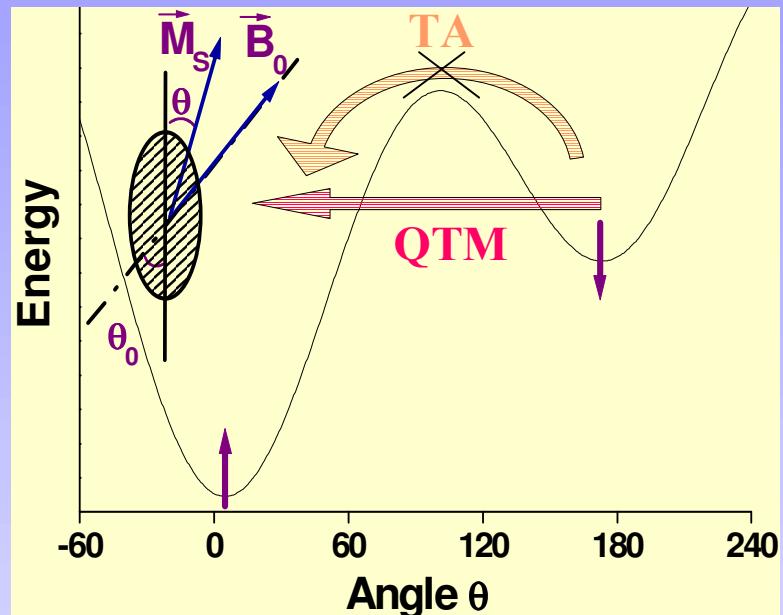
or diluted

➤ Inhomogeneous magnetic behavior

- ↳ *Pining of a narrow domain wall*
 - ↳ *Spin glass*
- ?

Problematic

$$E(\theta) = K \sin^2 \theta - M_s B_0 \cos(\theta_0 - \theta)$$

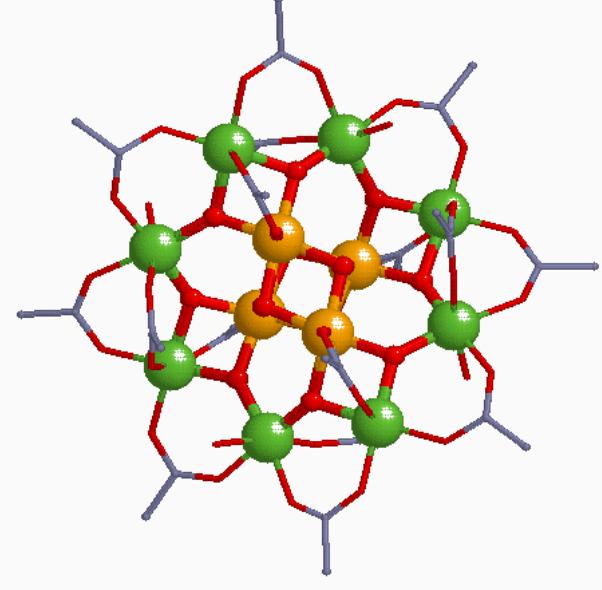


$+M_s$ 0 $-M_s$

- Thermal activation
↳ below T_B , $\tau_{TA} \geq \tau_{exp}$
- Slow quantum fluctuations
↳ Mesoscopic spin ($S \sim 10$)
 - $H = H_1 + H_2$
 - $[H_1, S_Z] = 0$
 - $[H_2, S_Z] \neq 0 \rightarrow i\hbar \partial \psi / \partial t \neq 0$
 - level separations
 - axial anisotropy
 - level repulsions
 - time evolution
(QTM)
 - axial symmetry breaking

Mesoscopic spins

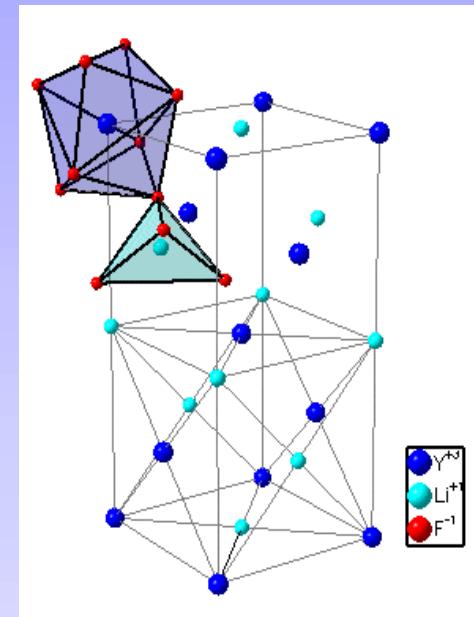
Single molecule magnets



$S = 10$

Diluted rare-earth ions

$\text{LiY}_{1-x}\text{Ho}_x\text{F}_4$

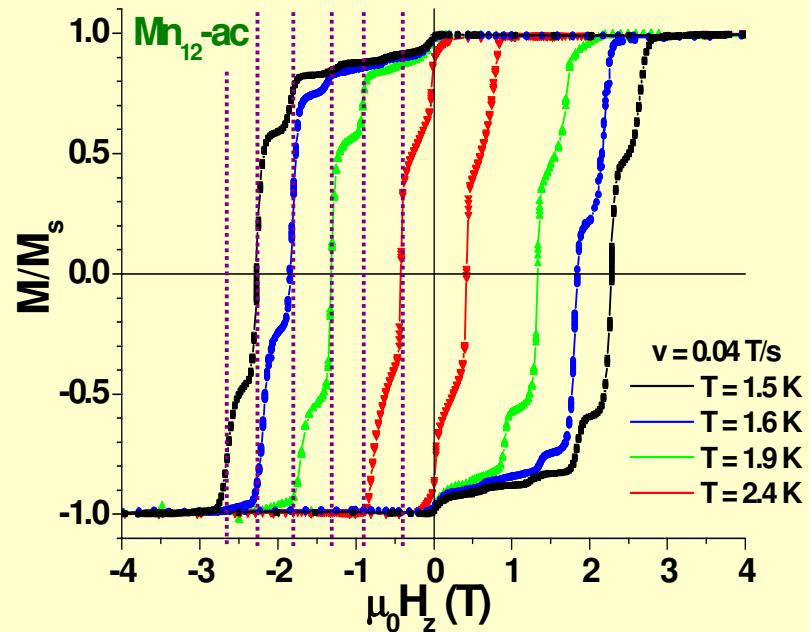


$J = 8$

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Mesoscopic spins

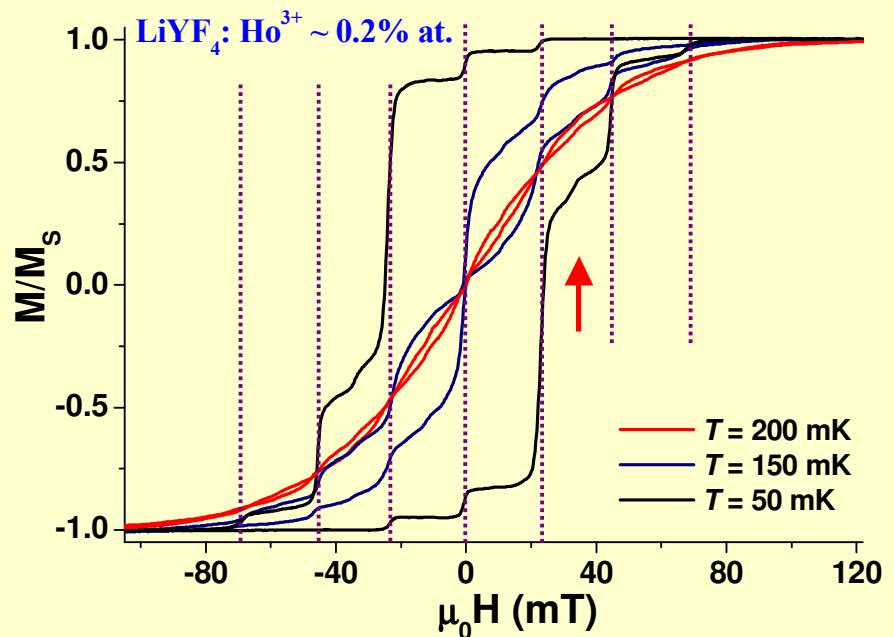
Single molecule magnets



$$\mu_0 H_n \approx n \times 0.4 \text{ T} \quad (n \text{ integer})$$

L. Thomas et al., Nature 383, 145 (1996)

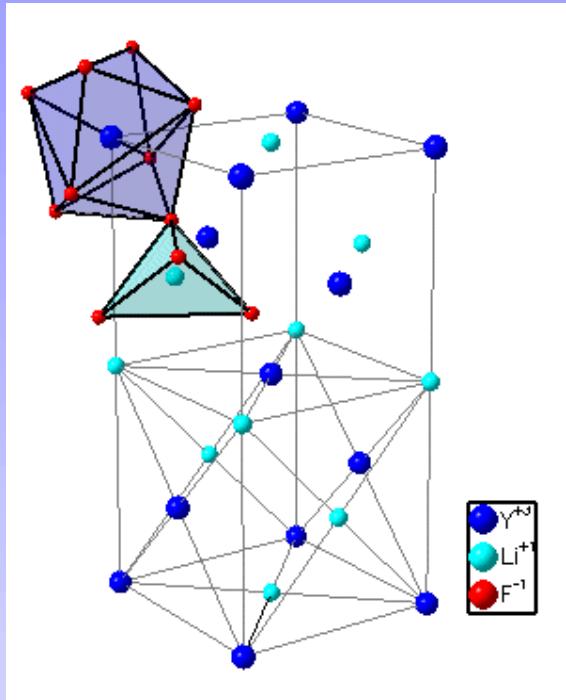
Diluted rare-earth ions



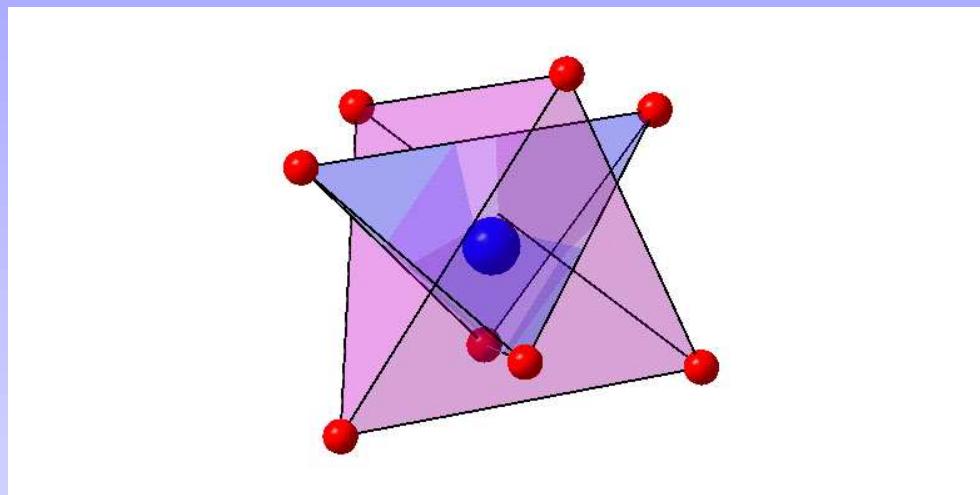
$$\mu_0 H_n \approx n \times 23 \text{ mT} \quad (n \text{ integer})$$

R. Giraud et al., PRL 87, 057203 (2001)

LiY_{1-x}Ho_xF₄ a model system



- Free ion $J=8 \rightarrow 2J+1 = 17 \quad |J,M\rangle$
 - Crystal field point symmetry S_4 IR: $\Gamma_1, \Gamma_2, \Gamma_3, \Gamma_4$

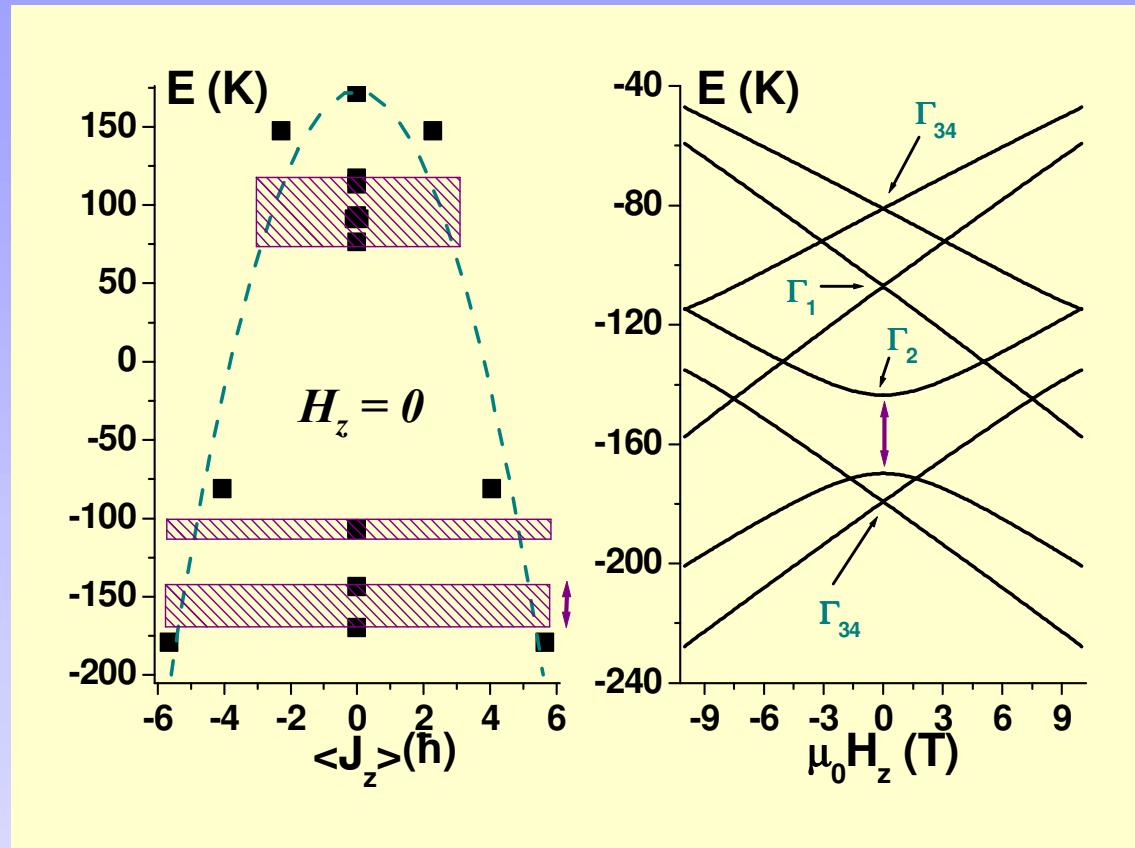


$$H_{CF} = B_{20}O_{20} + B_{40}O_{40} + B_{60}O_{60} + B_{44}O_{44} + B_{64}O_{64}$$

level separations

level mixings

Electronic Zeeman diagram



➤ Thermal activation

$$T_1(T) \rightarrow T_B$$

$$\text{Orbach } T_1 \propto e^{\delta E/kT}$$

$$\delta E \sim 10\text{K}$$

➤ Slow quantum fluctuations

Ising-like ground doublet

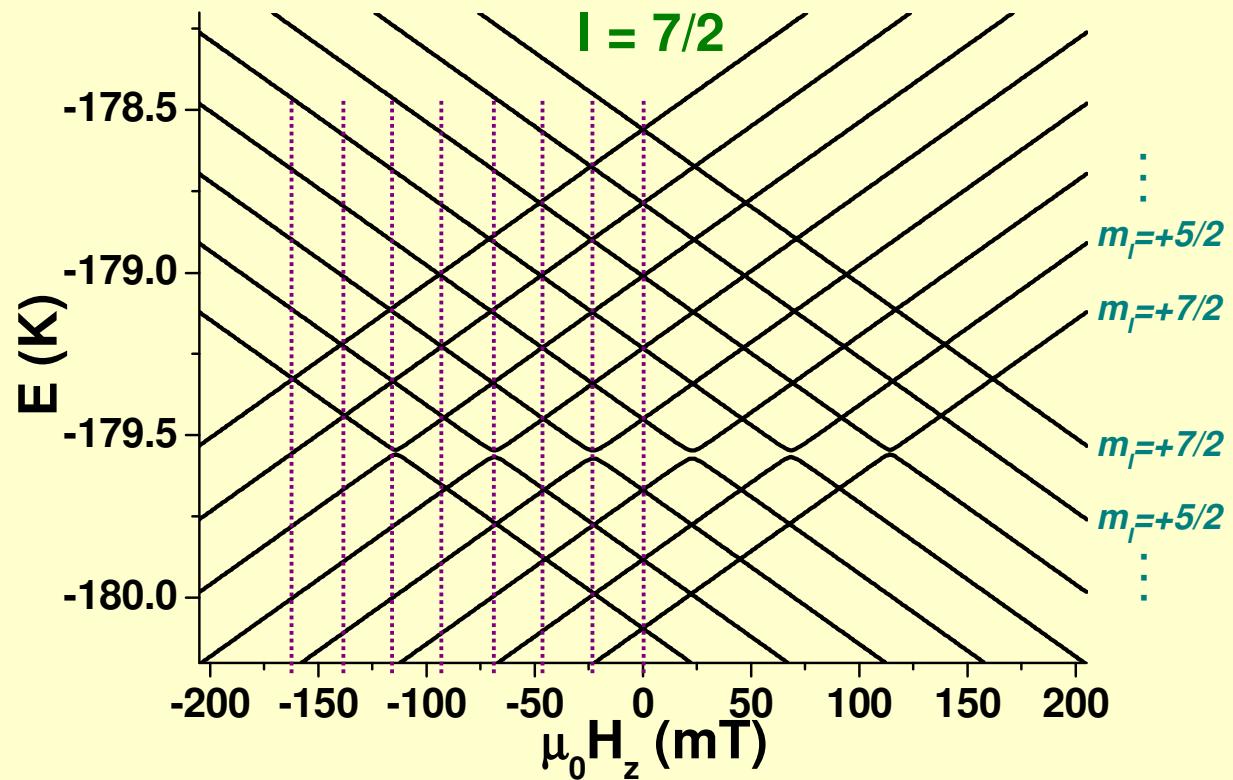
$$S=1/2 \text{ with } g_{\text{eff}} \sim 13$$

Stability of this doublet...?

↳ Holmium **nuclear spin**

Strong hyperfine coupling limit

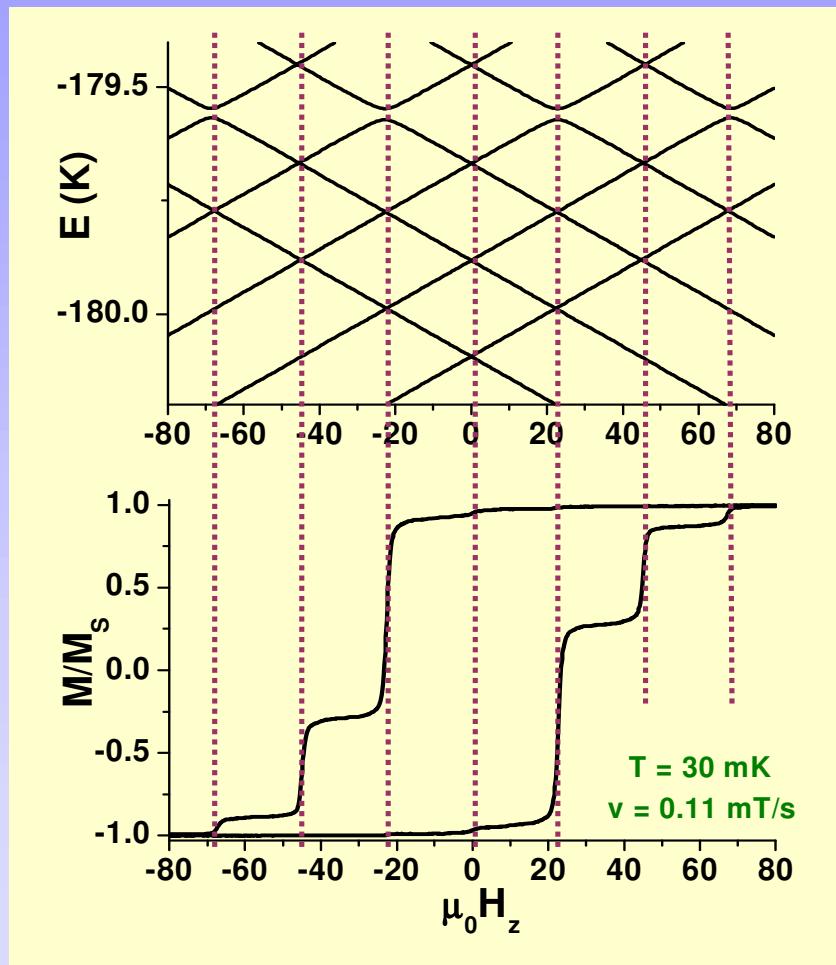
$H = H_{CC} + A_J \vec{J} \cdot \vec{I}$
 $A_J [J_z I_z + \frac{1}{2}(J_+ I_- + J_- I_+)]$
 $17 * 8 = 136$
 Hyperfine structure of the doublet → (16)
 $\delta E \sim 205 \text{ mK}$



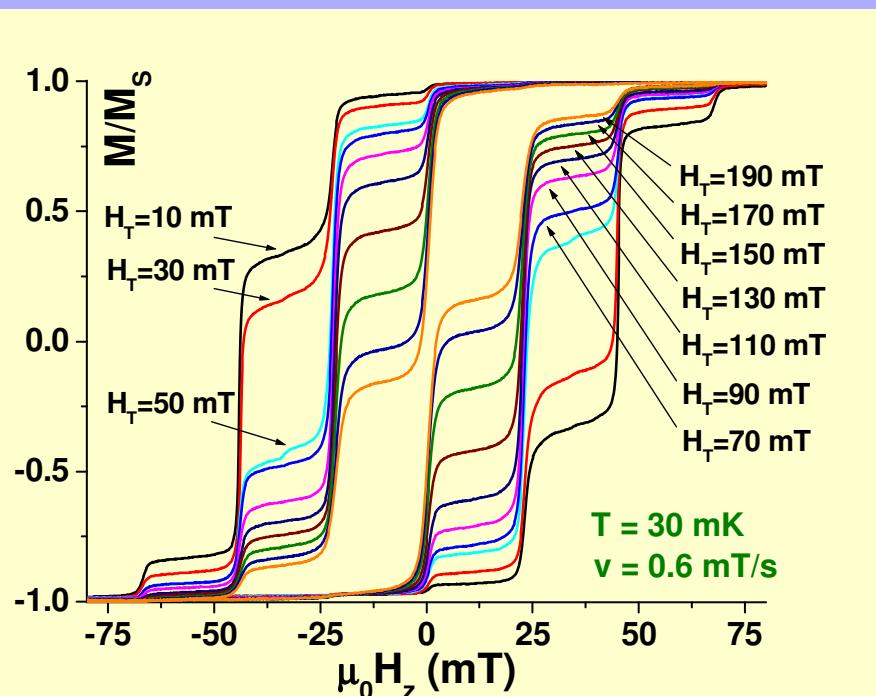
Resonance fields : $\mu_0 H_n \approx n \times 23 \text{ mT}$ ($-7 \leq n \leq +7$)

*The quantum dynamics of a **single** Ho³⁺ ion*

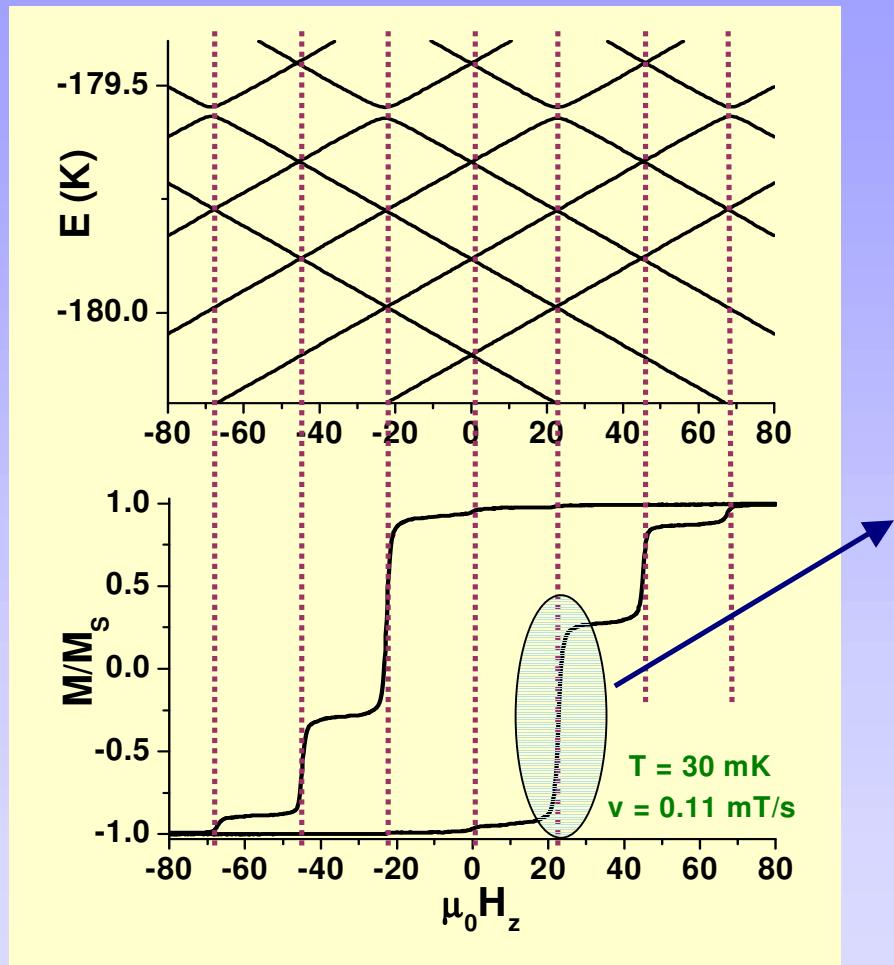
@ slow field sweep rates ($v \sim 1\text{ mT/s}$)



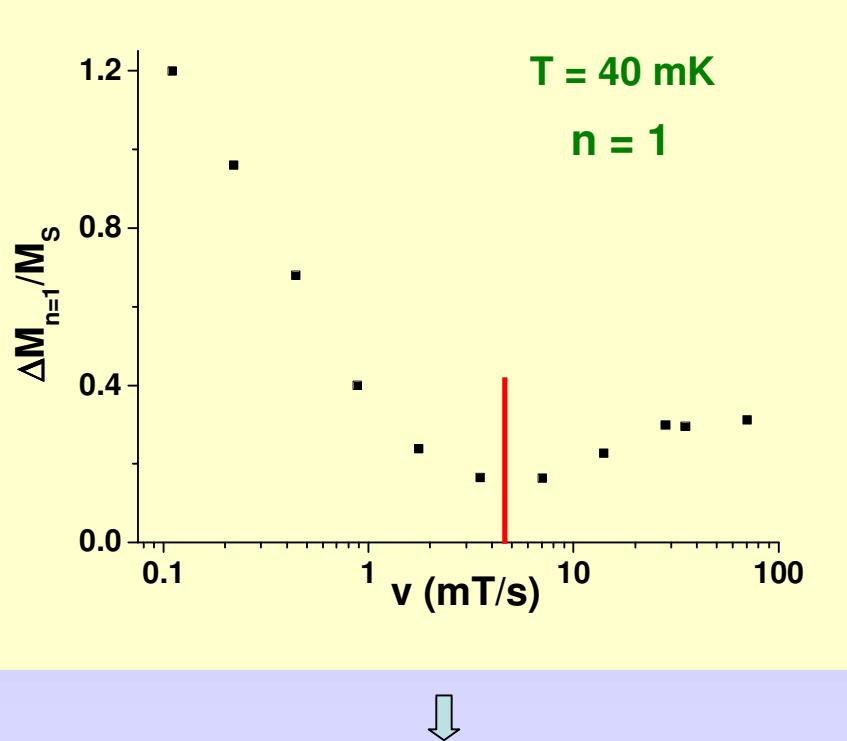
*Additional symmetry breaking
due to a **transverse field H_T***



*From the quantum dynamics of a **single** Ho³⁺ ion...
...to **many-body** effects*



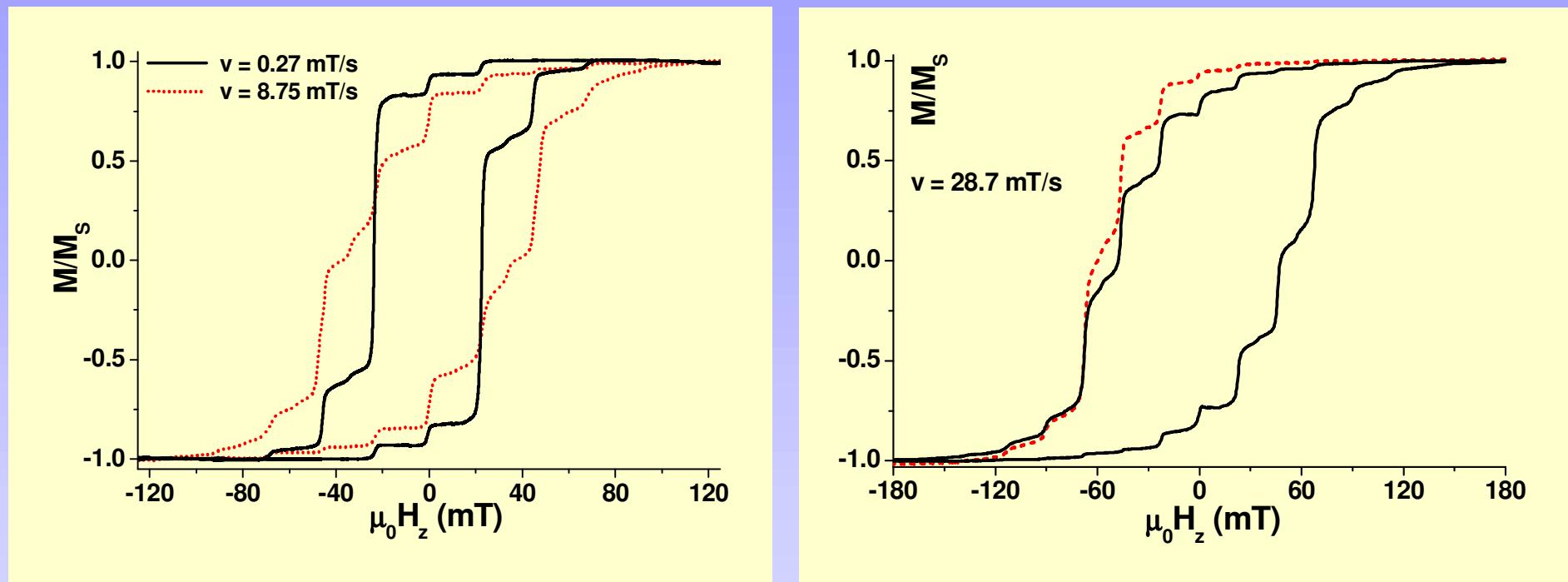
Field sweep rate dependence...



Crossover to a strongly
out-of-equilibrium spin system

Phonon bottleneck

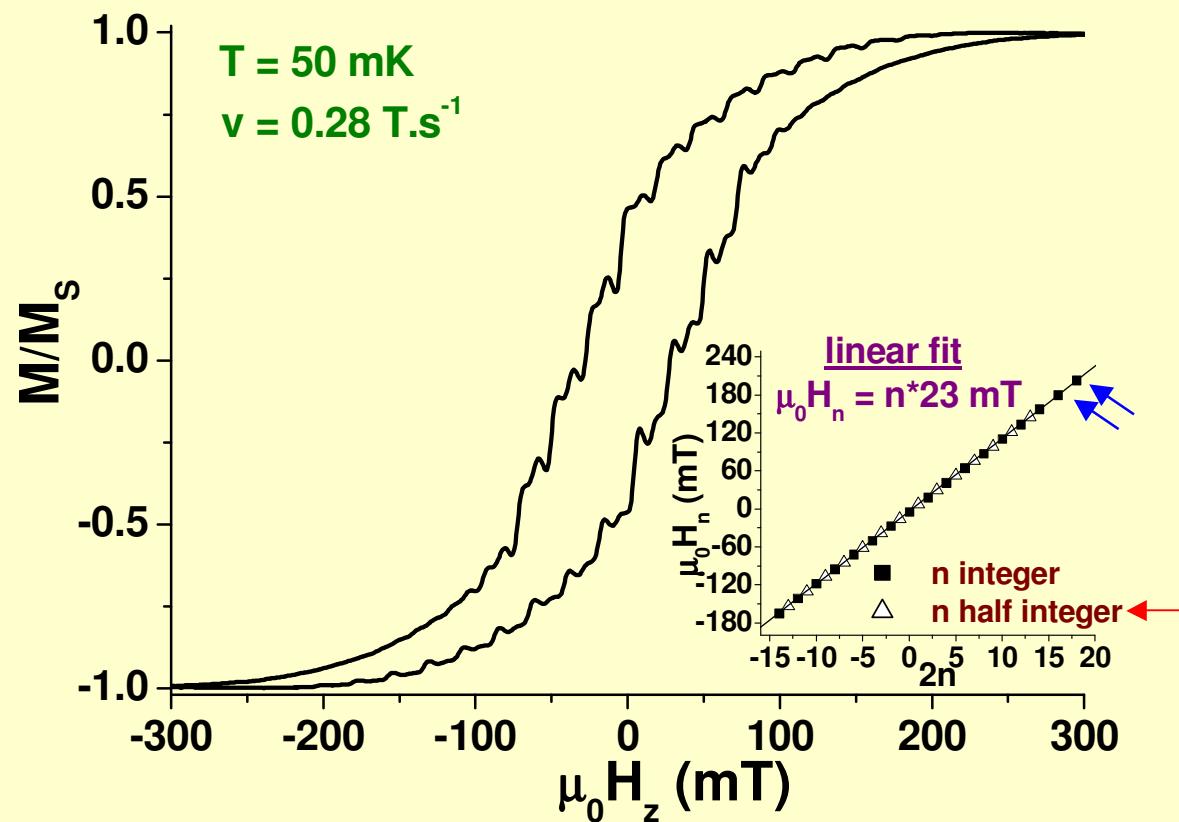
Raise of the internal temperature when increasing the sweep rate



*The field sweep drives the spin system
far from its internal equilibrium*

The quantum dynamics of an ensemble of Ho³⁺ ions

@ fast field sweep rates ($v \sim 1\text{ T/s}$)



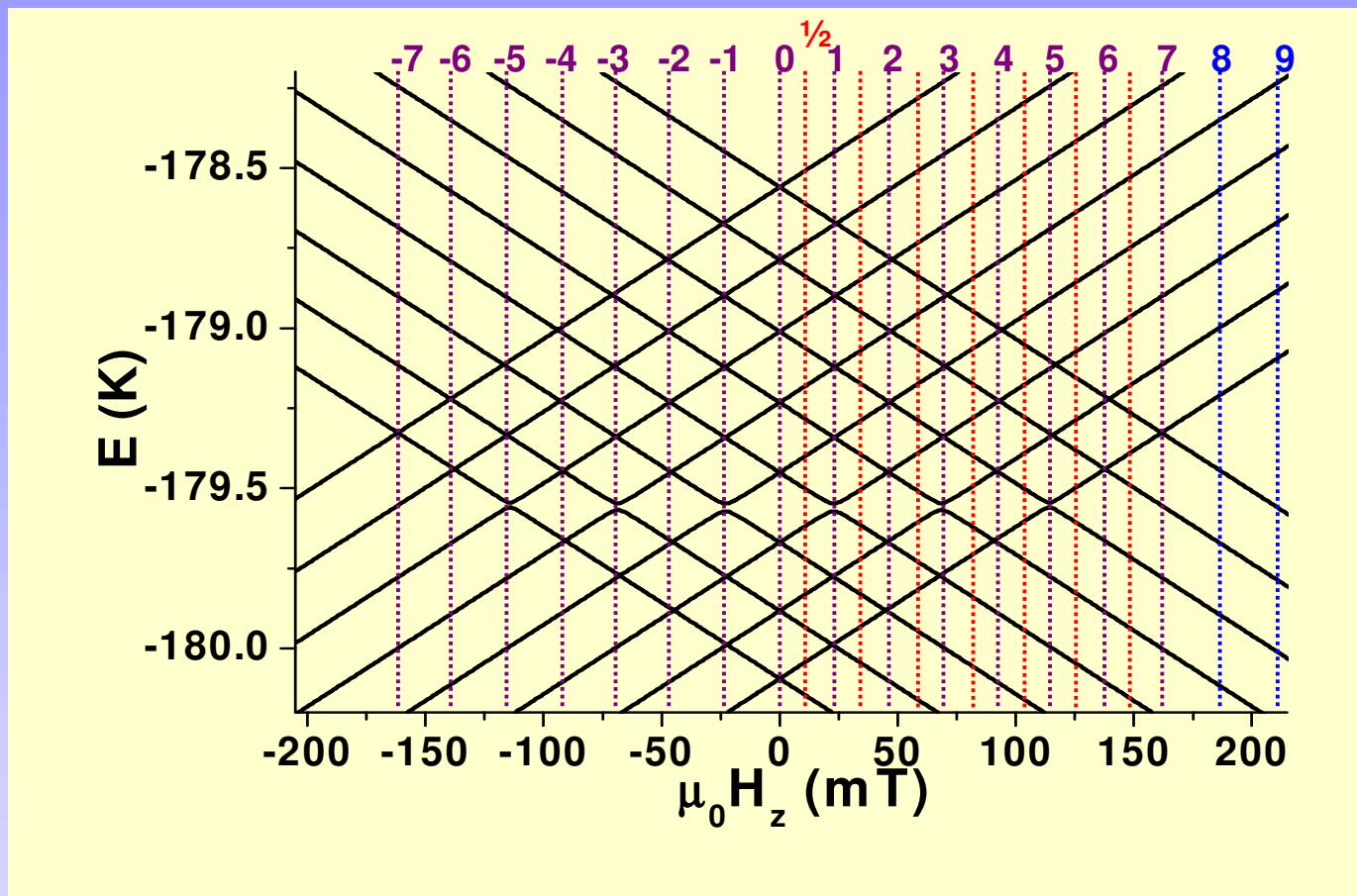
Additional magnetization steps

No explanation in terms of level crossings within the *single-ion representation*

$n = 8, 9$

$-13 \leq 2n \leq +13$
(n half integer)

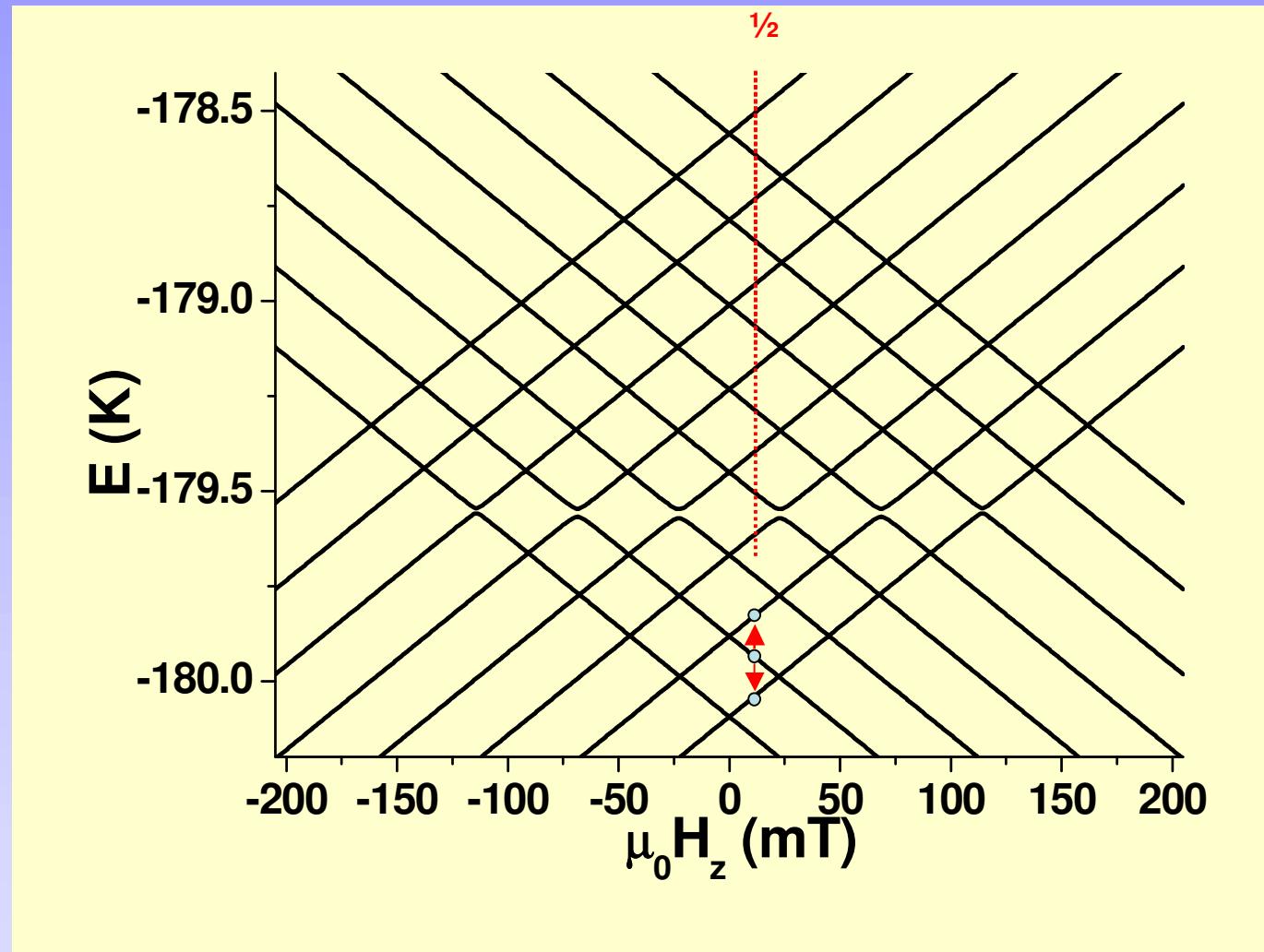
Spin-spin cross relaxations



No level crossings *but...* **equally-spaced levels**

Some multi-spins transitions allow for energy conservation @ resonant fields

Spin-spin cross relaxations: co-tunneling & biased tunneling



↑↑ Co-tunnel
↓↓ Biased
↑↓ tunneling

The two-ions representation

$$\mathbf{H} = \mathbf{H}^{(1)} + \mathbf{H}^{(2)} + \mathbf{H}^{12}$$

$$136 * 136 = \underline{18496}$$

Doublet Γ_{34}

$$J = 8 \Rightarrow S = \frac{1}{2}$$

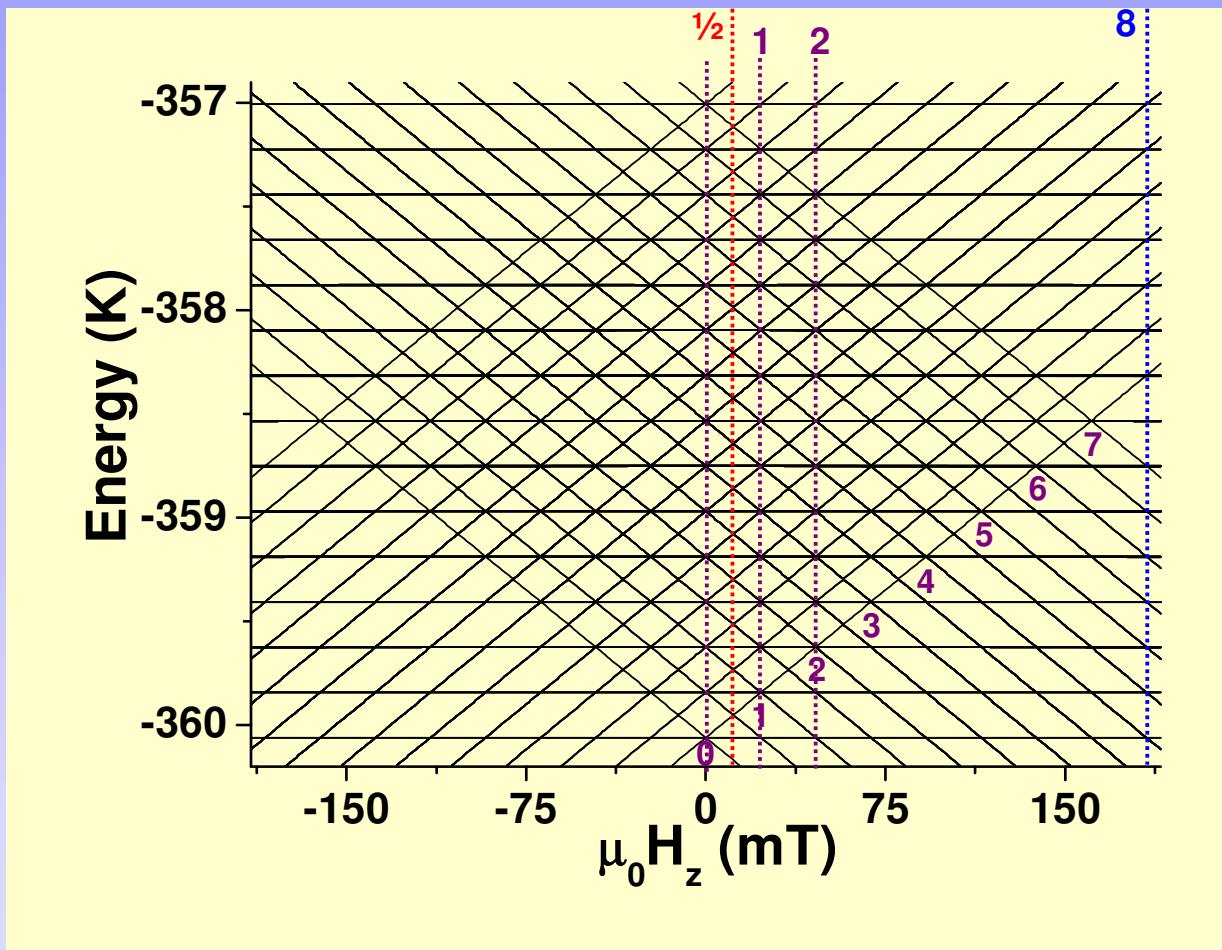
$$16 * 16 = \underline{256}$$

$$\mathbf{H}^{12} = 0$$

Doublet Γ_{34}

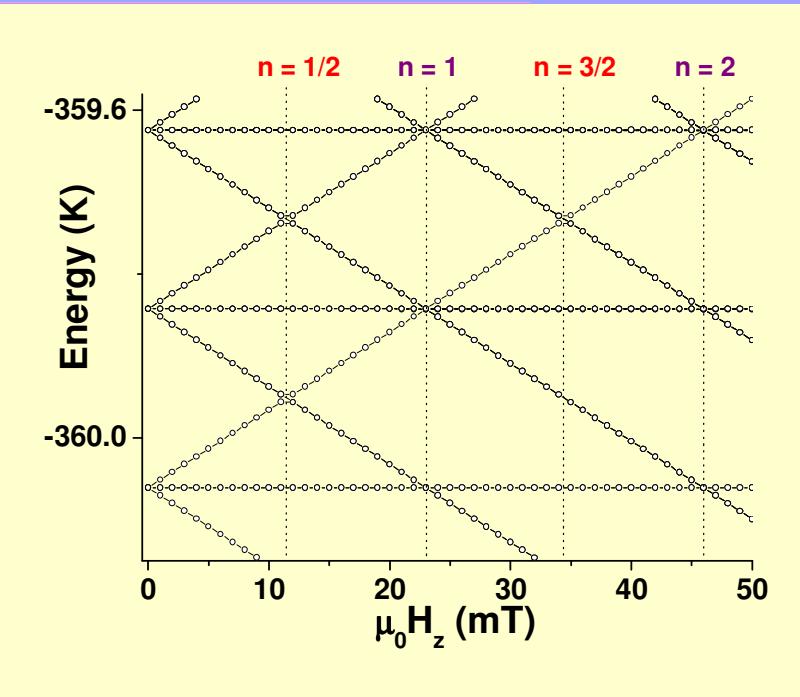
Singlet Γ_2

$$24 * 24 = \underline{576}$$

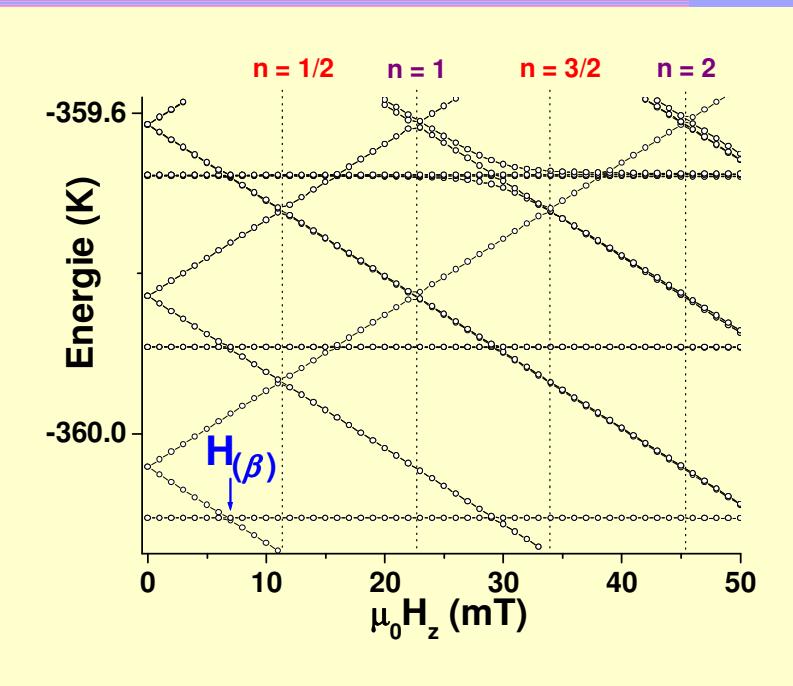


The two-ions representation

Without any coupling



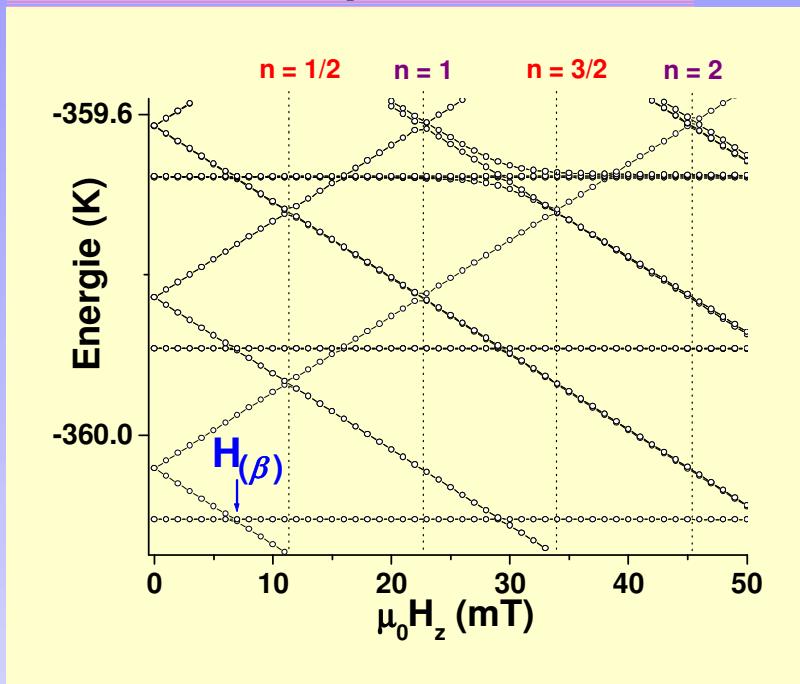
With an isotropic interaction



- Co-tunneling crossing fields are independent of the coupling strength β
(transitions are allowed by dipolar/anisotropic exchange interactions)
- Biased tunneling crossing fields (by a ‘molecular field’)
(fine structure *if* exchange couplings > dipolar interactions)

The two-ions representation

With an isotropic interaction



Co-tunneling transitions are allowed by anisotropic interactions

Dipole-dipole interactions

$$H_{\text{dip-dip}} = \frac{1}{2} \sum [g_k g_l \mu_B^2 / r_{kl}^3]$$

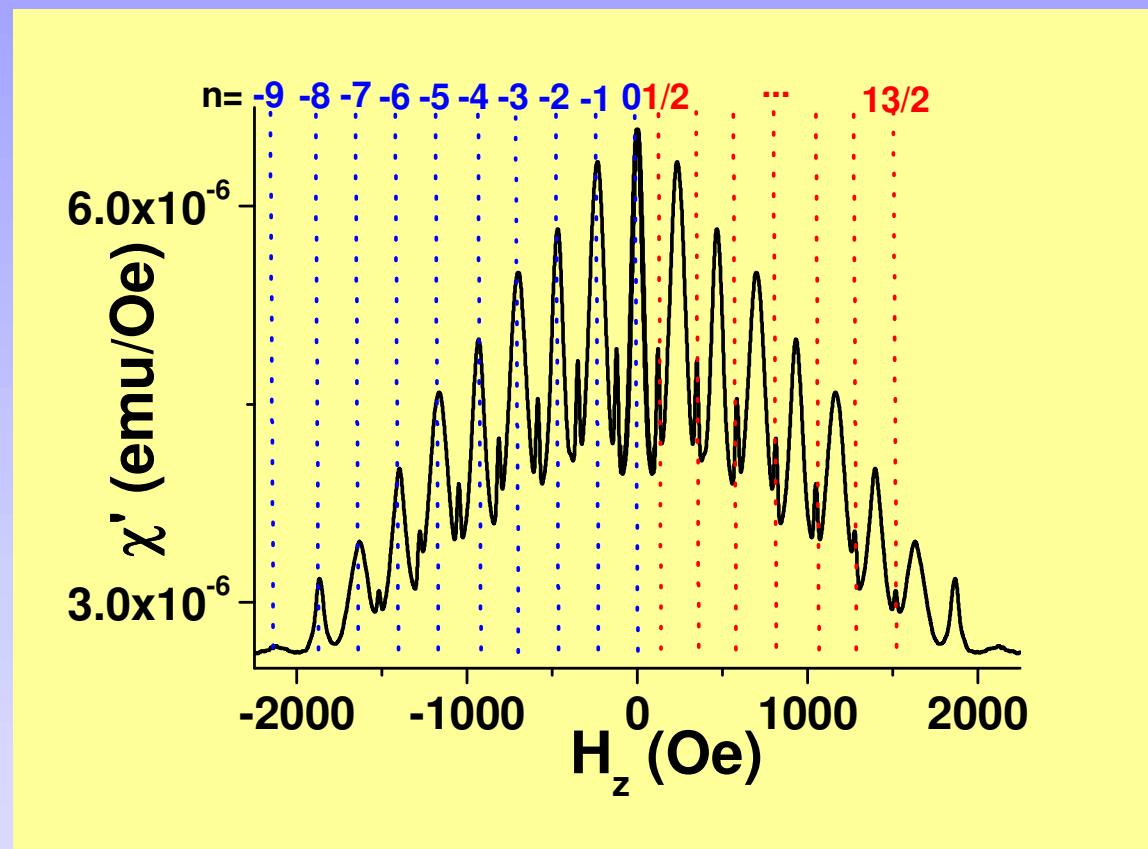
$$(1 - 3\cos^2\theta_{kl})[S_{zk} S_{zl}^{-1/4} (S_{+k} S_{-l} + S_{-k} S_{+l})]$$

$$-3/2\cos\theta_{kl}[e^{-i\phi} (S_{+k} S_{zl} + S_{zk} S_{+l}) + e^{-i\phi} (S_{-k} S_{zl} + S_{zk} S_{-l})]$$

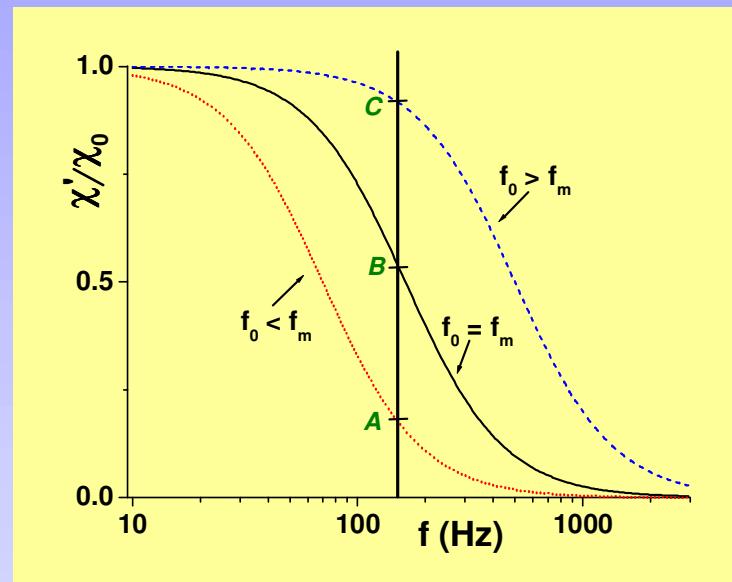
$$+^{3/4}\sin^2\theta_{kl}(e^{-i2\phi} S_{+k} S_{+l} + e^{-i2\phi} S_{-k} S_{-l})]$$

Ac-susceptibility measurements

@ higher temperatures ($T > 1.8\text{K}$)



Debye model

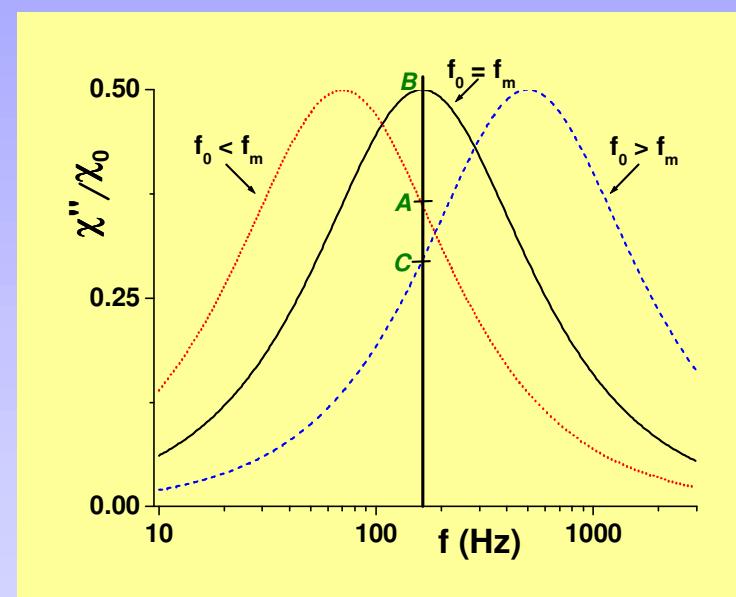
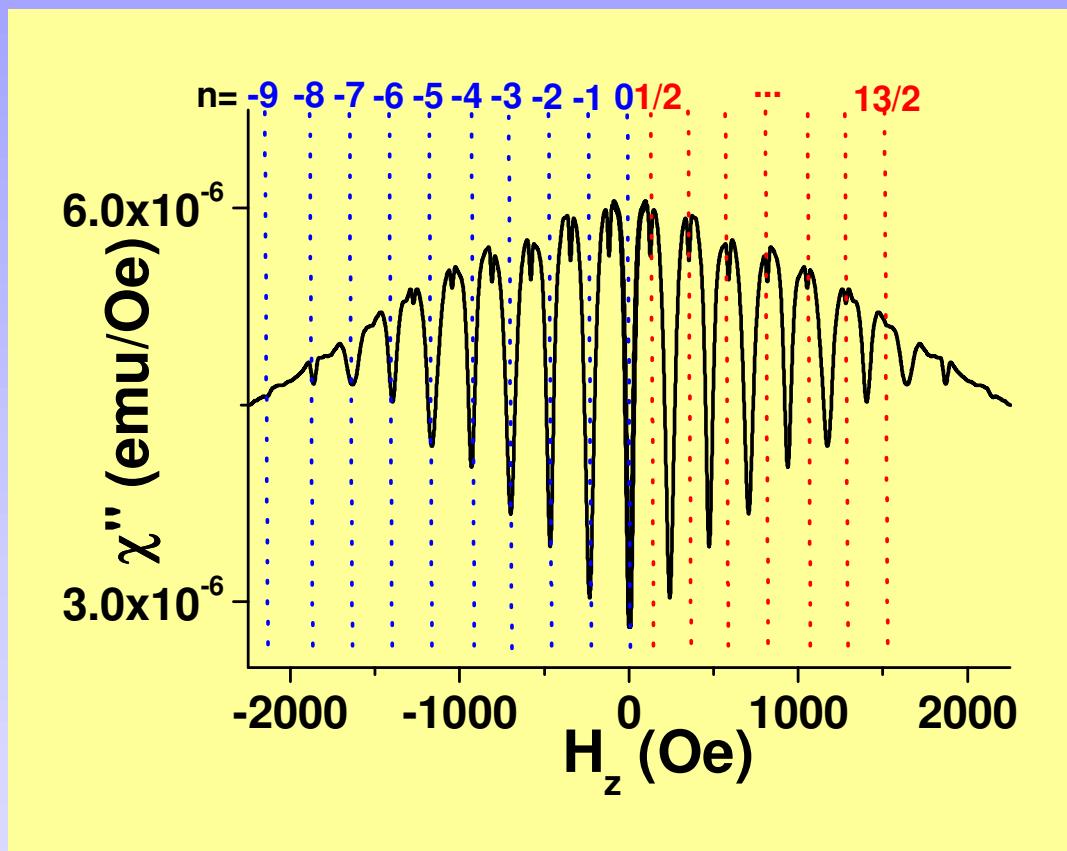


$f_0 (H_z)$

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Ac-susceptibility measurements

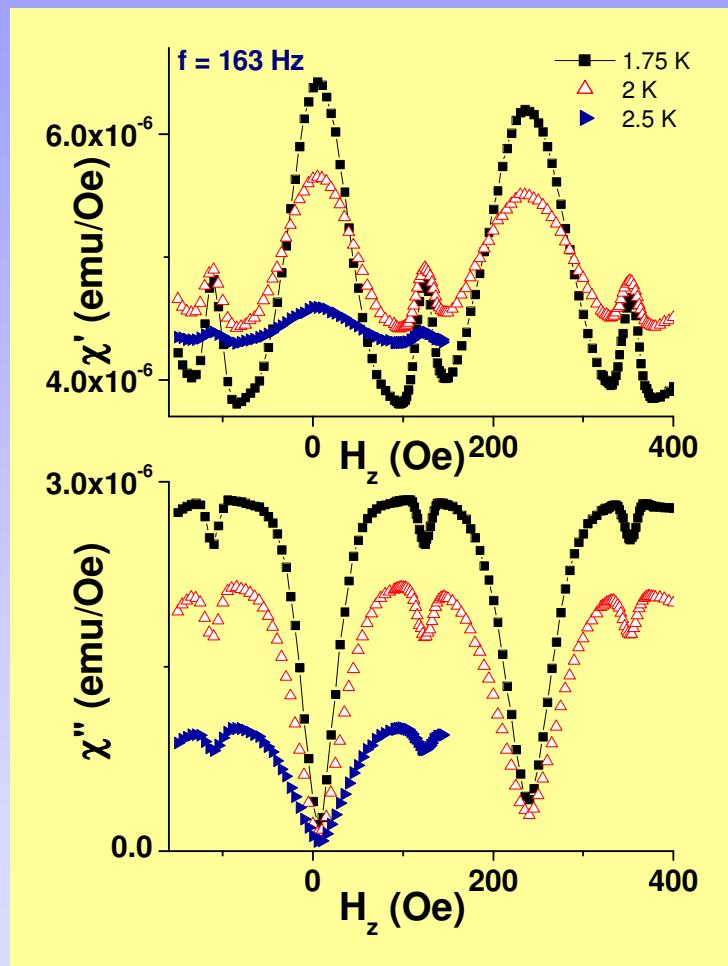
@ higher temperatures (T>1.8K)



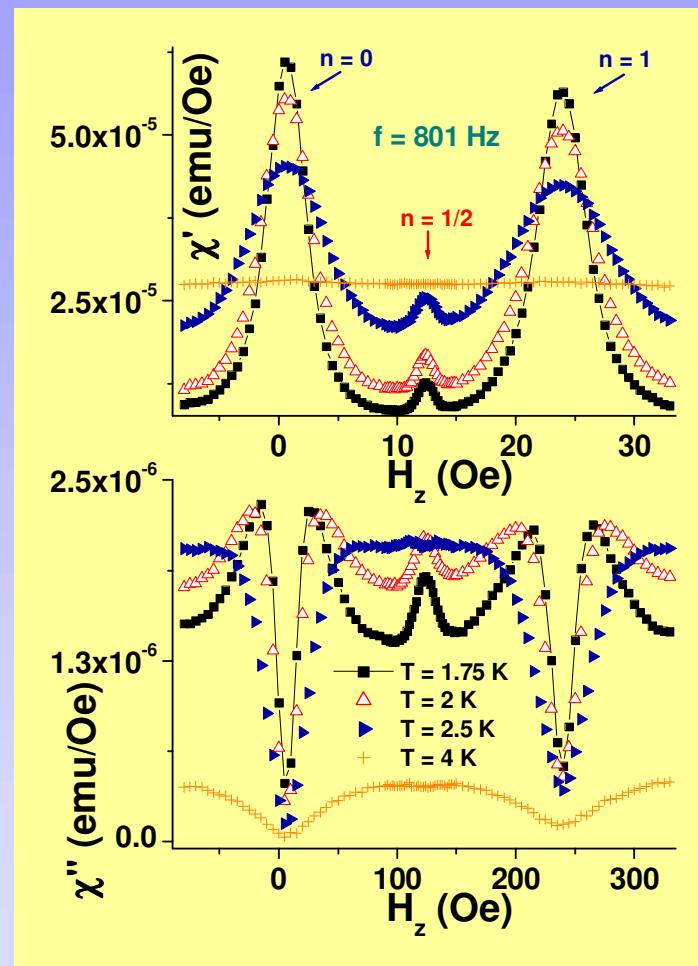
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Ac-susceptibility measurements

@ f = 163 Hz



@ f = 801 Hz



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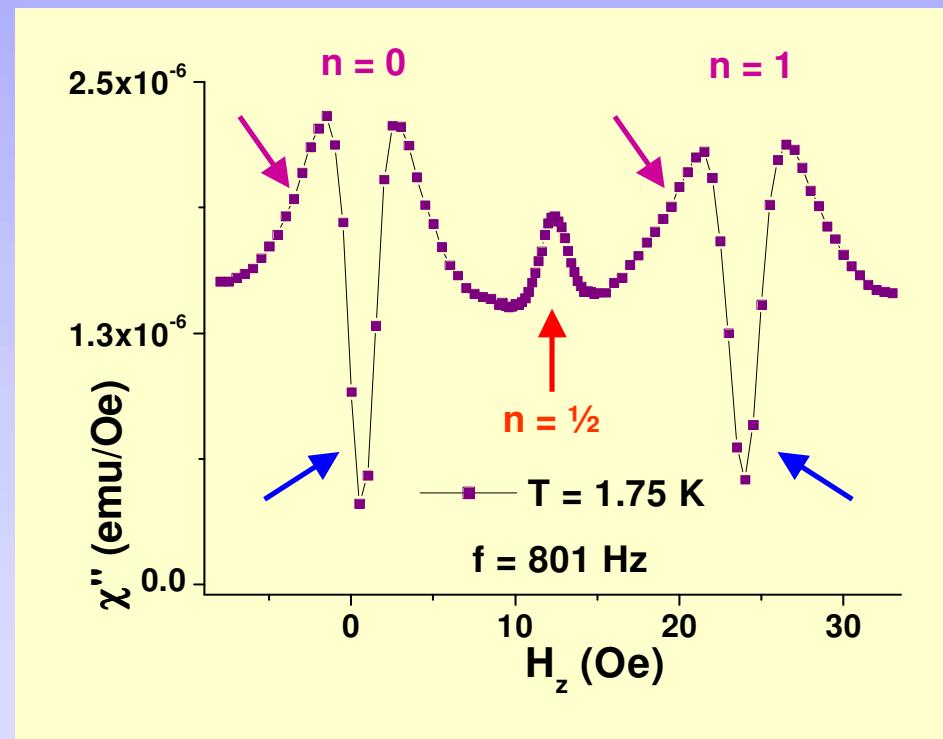
Ac-susceptibility measurements

$1.75 \text{ K} < T < 5 \text{ K}$

↳ Homogeneous phonon broadening > Inhomogeneous dipolar broadening

Allows to distinguish between
the various tunneling mechanisms

- Single-ion tunneling
- Two-ions co-tunneling
- Dipolar-biased tunneling



Spin-spin cross relaxations_u : a KEY ingredient ...

... to understand quantum fluctuations in an ensemble of interacting spins

- *Weakly coupled mesoscopic spins : Multi-spins dynamics*

- ↳ *Spin bath theory (Prokof'ev & Stamp)*

- ↳ *Co-tunneling dynamics @ fast field sweep rates*

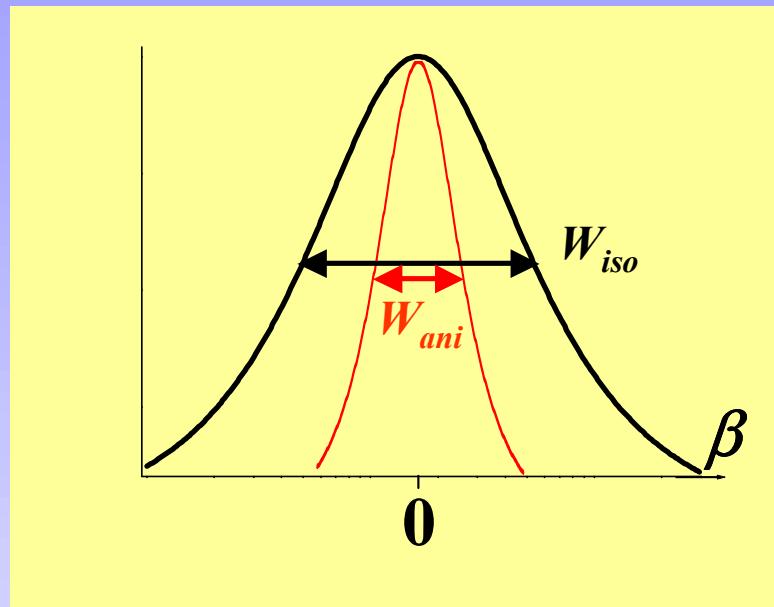
- *Spin glass*

- ↳ *Role of weakly interacting spins...?*

... Strength & Nature of the interaction...

Spin-spin cross relaxations: a KEY parameter ...

... to understand cross-spin relaxations...



$$R = \frac{W_{ani}}{W_{iso}}$$

Large R required to allow for quantum fluctuations at large scales...

Quantum spin glass

- ↳ *Dipolar spin glass*
- ↳ *Diluted magnetic semiconductors (hole-mediated exchange interactions)*

Summary

Highly diluted Ho^{3+} ions in LiYF_4
exhibit a **mesoscopic behavior** at low T



The measure of an **ensemble** demonstrate
various quantum relaxation mechanisms

- *Single-ion behavior* : *strong hyperfine coupling*
- *Many-body effects* : *co-tunneling & biased tunneling*
 - ↳ *Crucial role of anisotropic interactions
for quantum fluctuations at a large scale*

Thank you!

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