

Spin-orbit interaction, topology and electronic structure

Oleg Yazyev

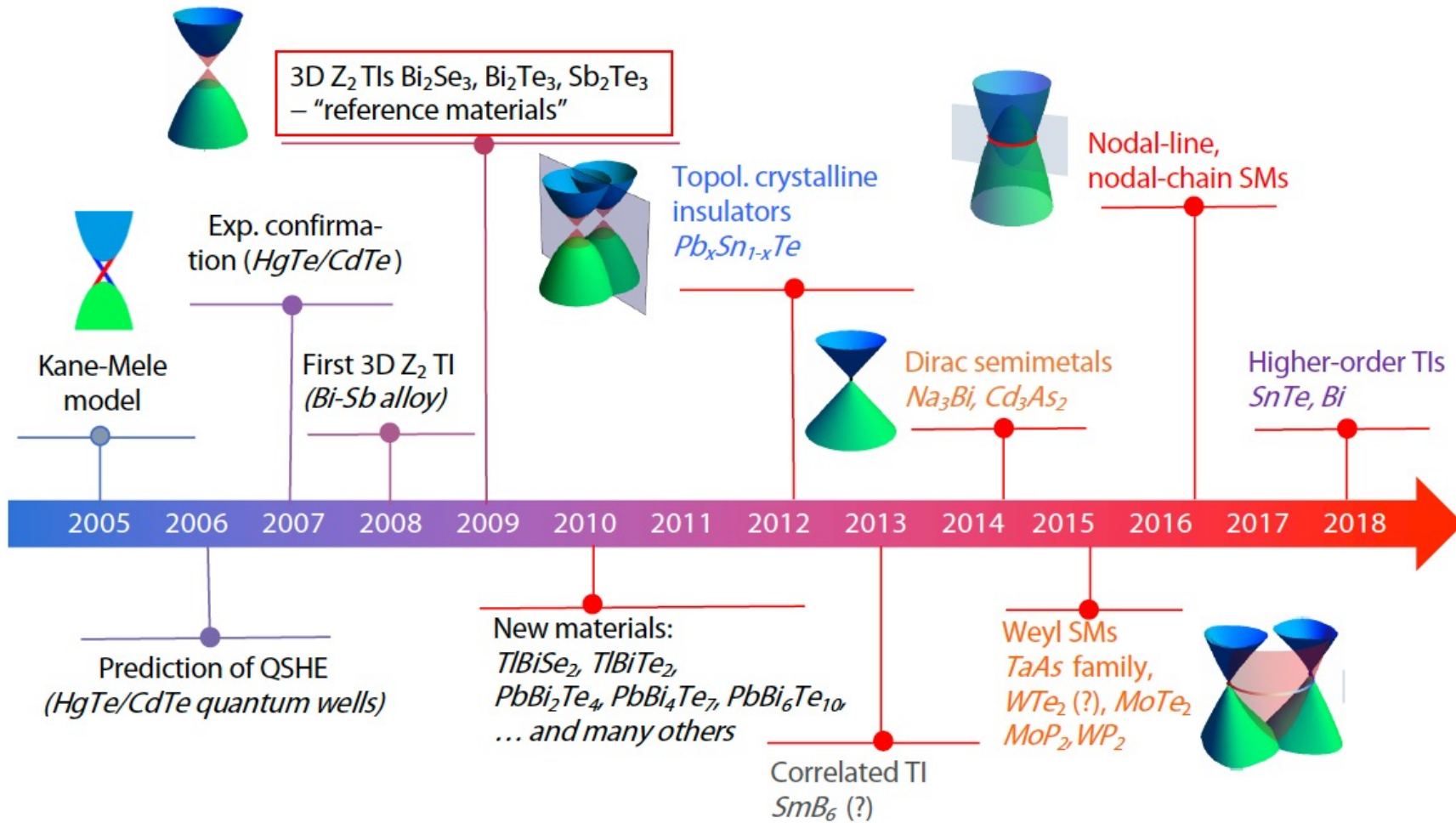
Chair of Computational Condensed
Matter Physics (C3MP)

Institute of Physics (IPHYS)

Ecole Polytechnique Fédérale de
Lausanne (EPFL)

Switzerland

Timeline of the field of topological materials



Talk outline

- Topological materials: brief introduction
- High-throughput search of novel topological materials
 - online database TopoMat <http://www.materialscloud.org/discover/topomat>
- Discovery of new materials – successful examples:
 - Bi₄I₄ topological insulator
 - G. Autès *et al.*, Nature Materials **15**, 154 (2016)
 - MoP₂ and WP₂ Weyl semimetals
 - G. Autès *et al.*, Phys. Rev. Lett. **117**, 066402 (2016)
- “Textbook” physical properties – magnetoresistance
 - S.N. Zhang, Q.S. Wu, Y. Liu, O. V. Yazyev, Phys. Rev. B **99**, 035142 (2019)
- Topological degeneracies and Fermi arcs in ordinary bcc iron
 - D. Gosálbez-Martinez, G. Autès, O. V. Yazyev, Phys. Rev. B **102**, 035419 (2020)

Quantum Hall effect and Chern number

Bloch wavefunction: $\Psi_k(r) = e^{ikr} u_k(r)$

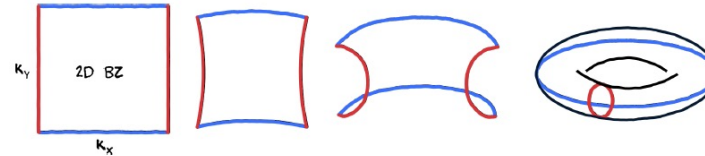
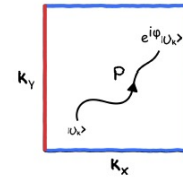
Berry connection: $A(k) = i\langle u_k | \nabla_k | u_k \rangle$

Berry phase: $\phi = \int_{\mathcal{P}} A(k) dk$

Berry curvature: $B(k) = \nabla_k \times A(k)$

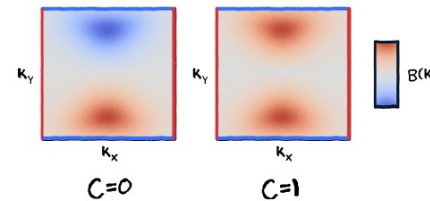
Theorem

The integral of $B(k)/2\pi$ over a closed surface is an integer \mathcal{C} .

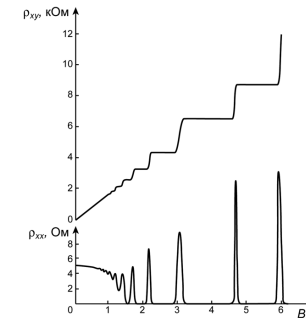
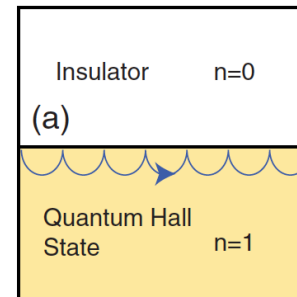


Chern number:

$$\mathcal{C} = \frac{1}{2\pi} \int_{2D\text{ BZ}} B(k) dk \in \mathbb{Z}$$

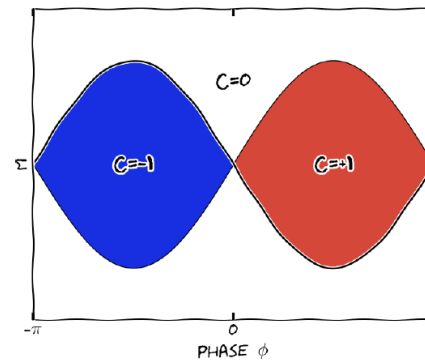
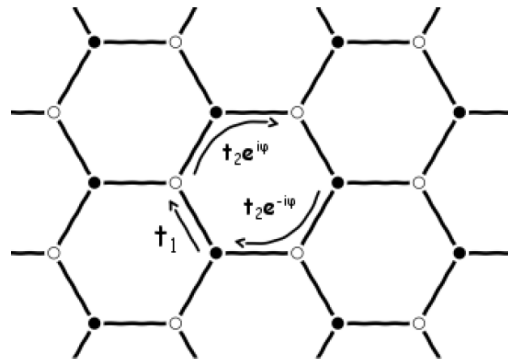


Integer quantum Hall effect (1980)



Haldane model

$$H = \sum_i M\tau_z c_i c_i^\dagger + \sum_{\langle i,j \rangle} t_1 c_i c_j^\dagger + \sum_{\langle\langle i,j \rangle\rangle} t_2 e^{i\tau_z \phi} c_i c_j^\dagger$$



Haldane, Phys. Rev. Lett. **61**, 2015 (1988)

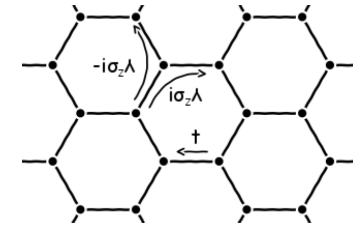
- breaks time-reversal symmetry
- chiral edge states
- integer quantum Hall effect without magnetic field (Chern insulator)

Quantum spin Hall effect

- Kane-Mele model – quantum spin Hall effect

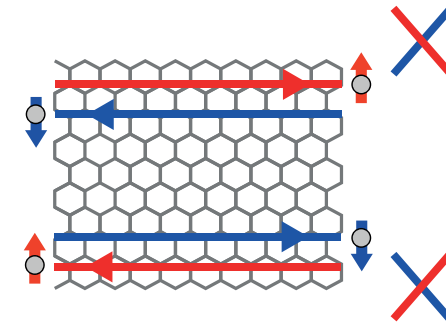
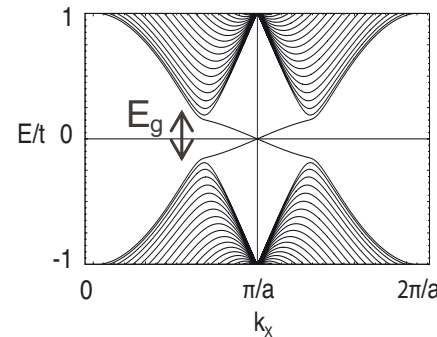
$$H = \sum_{\langle i,j \rangle} t c_{i\sigma} c_{j\sigma}^\dagger + \sum_{\langle\langle i,j \rangle\rangle} i\lambda \nu_{ij} c_i \sigma_z c_j^\dagger$$

- Z_2 topological invariant $\nu = \frac{C_\uparrow - C_\downarrow}{2} \in \{0, 1\}$



Kane & Mele, PRL 95, 226801 (2005)

- Corresponds to graphene + spin-orbit coupling (SOC)

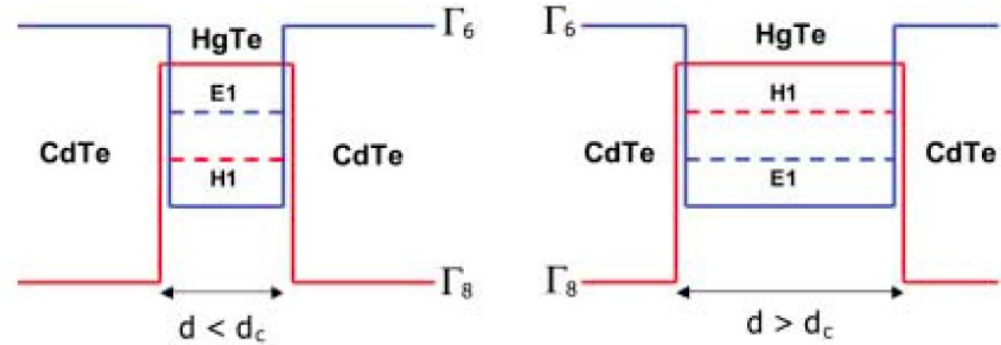
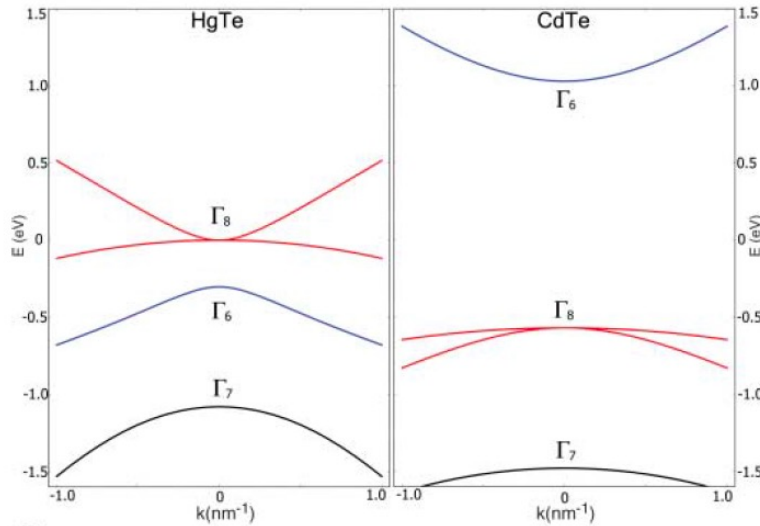


- However, SOC is too weak in graphene ($E_g = 25 \mu\text{eV}$)
- QSHE predicted and observed in HgTe/CdTe QWs

Bernevig *et al.* '06
Koenig *et al.*, '07

QSHE in HgTe quantum wells

2006: Prediction of quantum spin Hall effect in HgTe/CdTe QWs

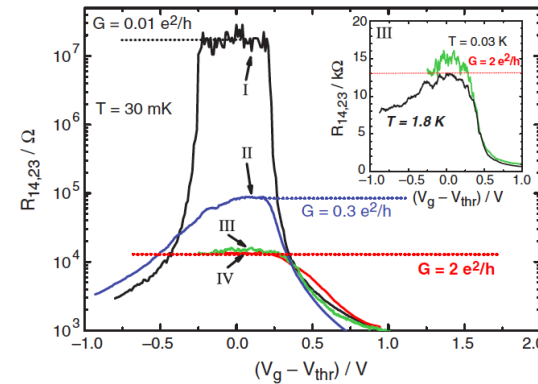


Bernevig *et al.*, Science **314**, 1757 (2006)

2007: Experimental confirmation (transport)

$$G = \frac{2e^2}{h}$$

Koenig *et al.*, Science **318**, 766 (2007)



Z_2 topological insulators

- Z_2 invariant ν (with inversion symmetry)

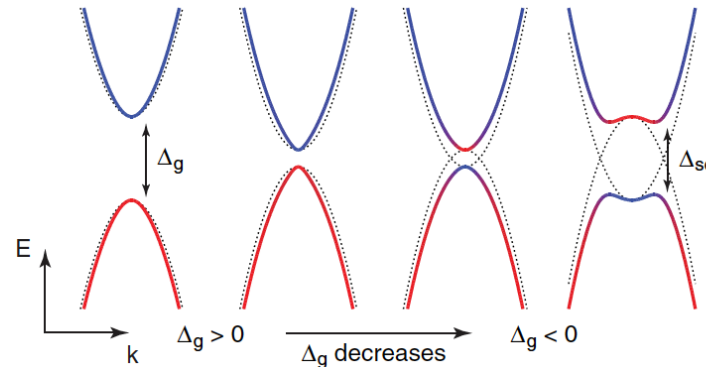
$$(-1)^\nu = \prod_{a=1}^{2^d} \delta_a \quad \delta_a = \prod_m \xi_m(\Lambda_a)$$

Λ_a - time-reversal invariant momentum (TRIM) points

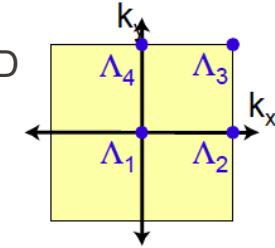
ξ_m - wavefunction parity

- Basic topological insulator (TI) recipe:

- Band inversion involving states of different parity
- Band gap open by spin-orbit interactions



TRIM points in 2D



Fu and Kane (2007)

Z2Pack approach

Hybrid Wannier function: wannierisation along one direction only:

$$|R_x k_y n\rangle = \frac{1}{2\pi} \int e^{-iR_x k_x} |\psi^{n, \vec{k}}\rangle dk_x$$

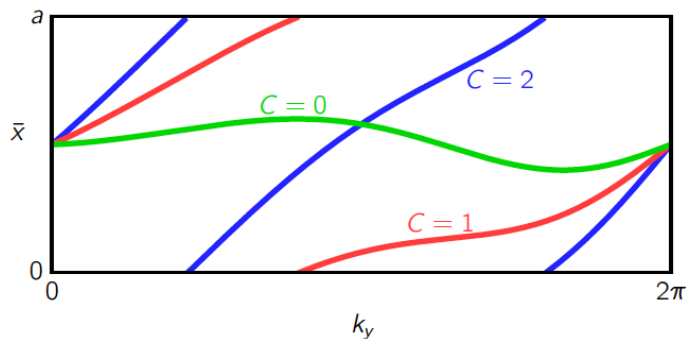
The Hybrid Wannier charge center...

$$\bar{x}(k_y) = \langle 0k_y n | x | 0k_y n \rangle$$

... is directly related to the Berry connection

$$\bar{x}(k_y) = \frac{ia_x}{2\pi} \int \langle u_{nk} | \partial_{k_x} | u_{nk} \rangle dk_x = \frac{a_x}{2\pi} \int \mathcal{A}_x(k_y) dk_x$$

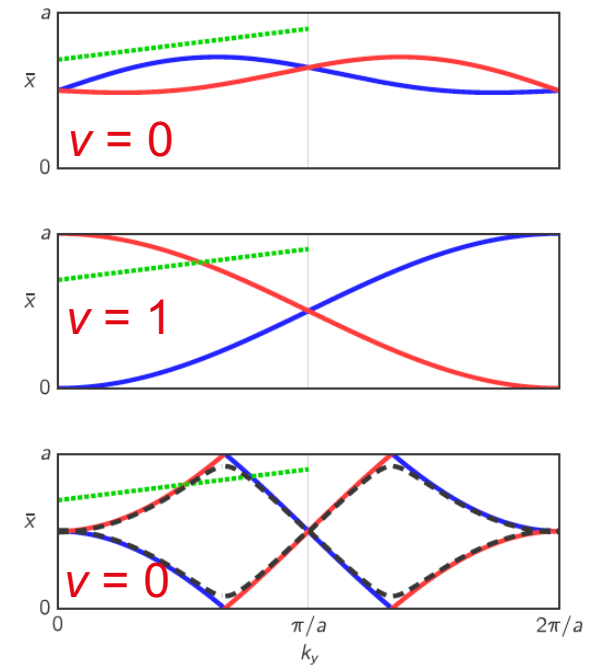
Chern number



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Z₂ index



Soluyanov & Vanderbilt, PRB'11, PRB'12
Gresch *et al.*, PRB 95, 075146 (2017)

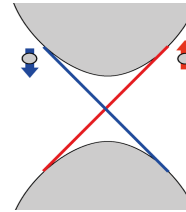
Z_2 topological insulators

- 2D TI - quantum **spin** Hall insulator
 ν (= 0 or 1)

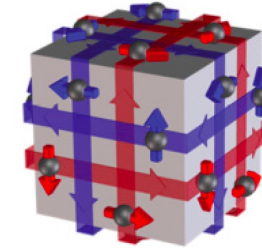
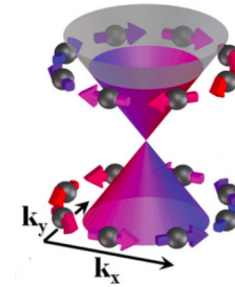
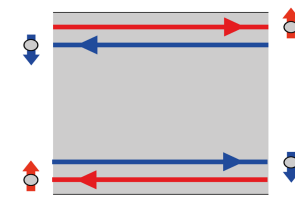
- 3D TI – crystalline materials
 $(\nu_0; \nu_1\nu_2\nu_3)$ – 16 topological classes

- consequences:
 - suppressed backscattering of charge carriers
 - charge current \Leftrightarrow spin polarization

k space



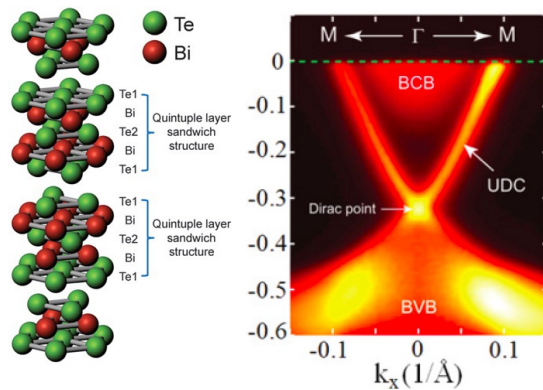
real space



First materials realizations of bulk TIs

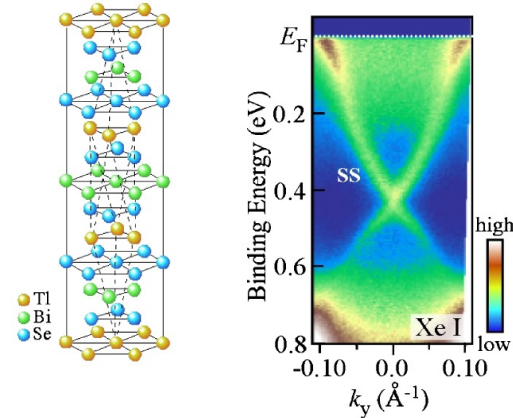
- similar structural motifs – Bi or Sb layered materials
- band gaps upto *ca.* 0.3 eV
- TI phase confirmed by observing surface states using ARPES
- similar surface-state dispersion – single Dirac cone at Γ

▪ Bi_2Se_3 , Bi_2Te_3



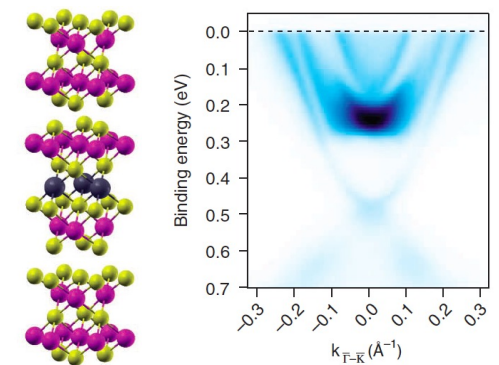
Xia *et al.*, Nature Phys. **5**, 398 (2009);
Zhang *et al.*, *ibid.* (2009)
figs from Chen *et al.*, Science'09

▪ TlBiSe_2



Sato *et al.*, PRL **105**, 136802 (2010)

▪ PbBi_4Te_7



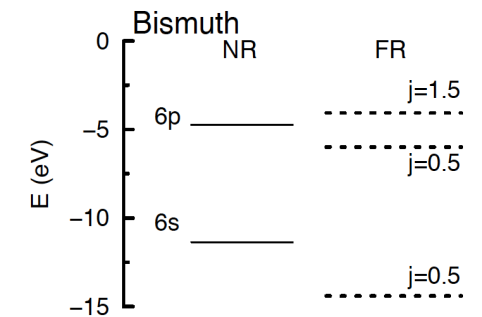
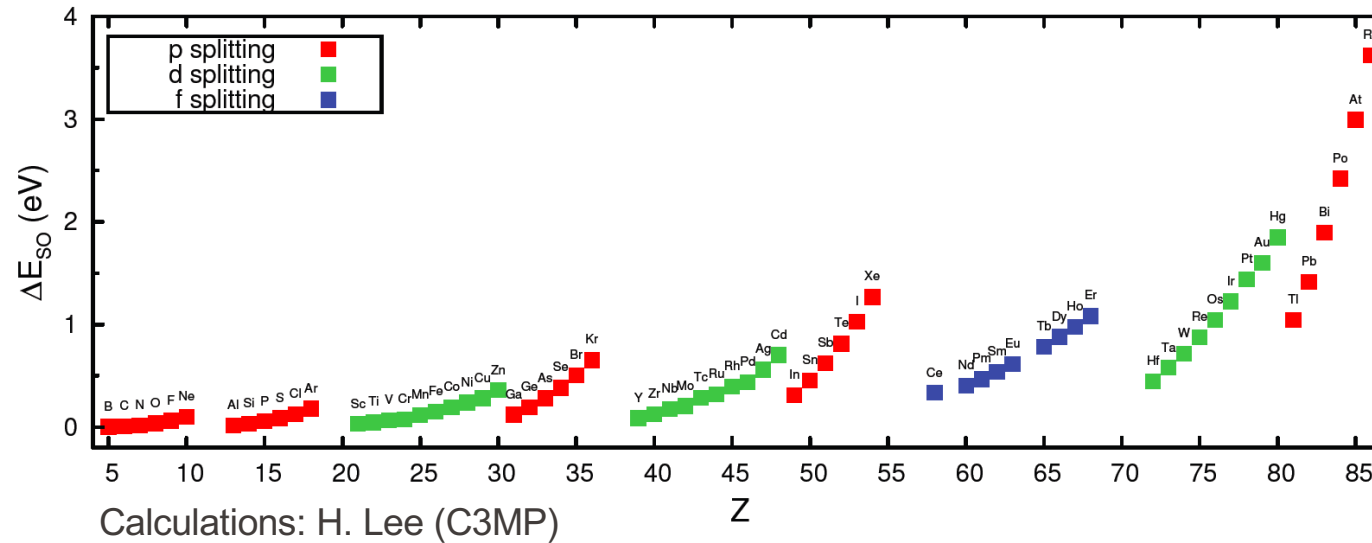
Eremeev *et al.*, Nat. Commun'12

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Spin-orbit interactions across periodic table

- spin-orbit coupling $\mathbf{H}_{\text{SO}} = \zeta \mathbf{L} \cdot \mathbf{S}$ is a relativistic effect
- in neutral atoms $\zeta \propto Z^2$ across the vertical direction of PT
(and not $\zeta \propto Z^4$ as often quoted, but the truth can be found in Landau-Lifshitz, as usual)
- faster growth across the horizontal dimension
- standard DFT calculations provide quantitative description



$$E_{6p}^{j=3/2} - E_{6p}^{j=1/2} = \frac{3}{2} \zeta_{6p} = 1.9 \text{ eV}$$

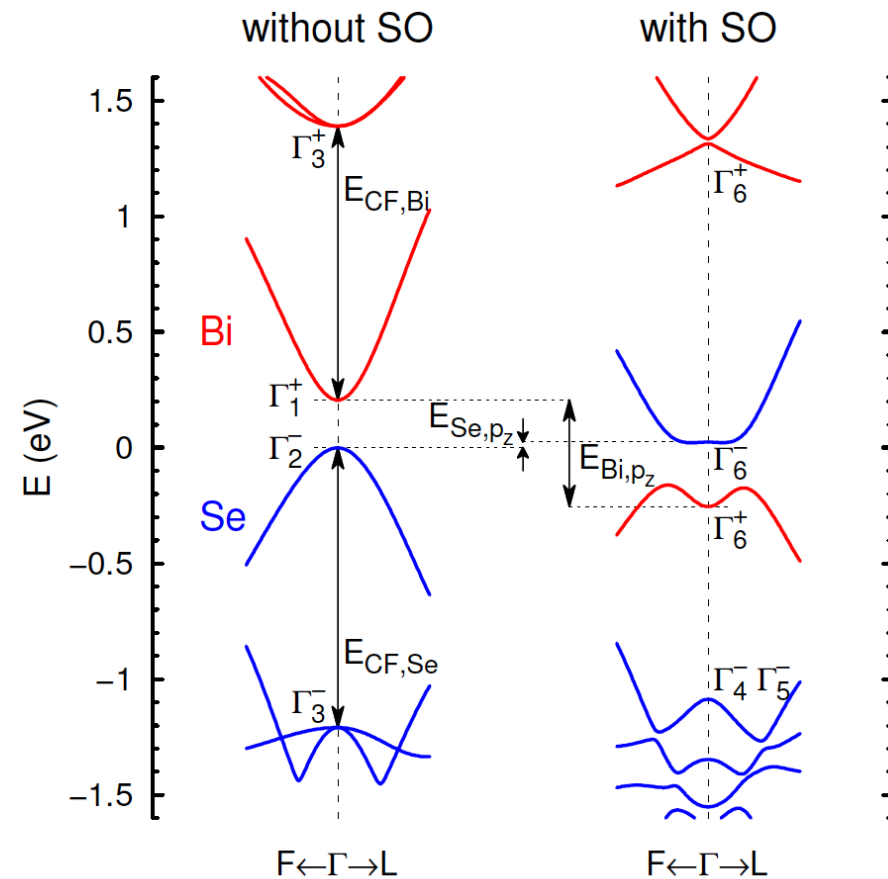
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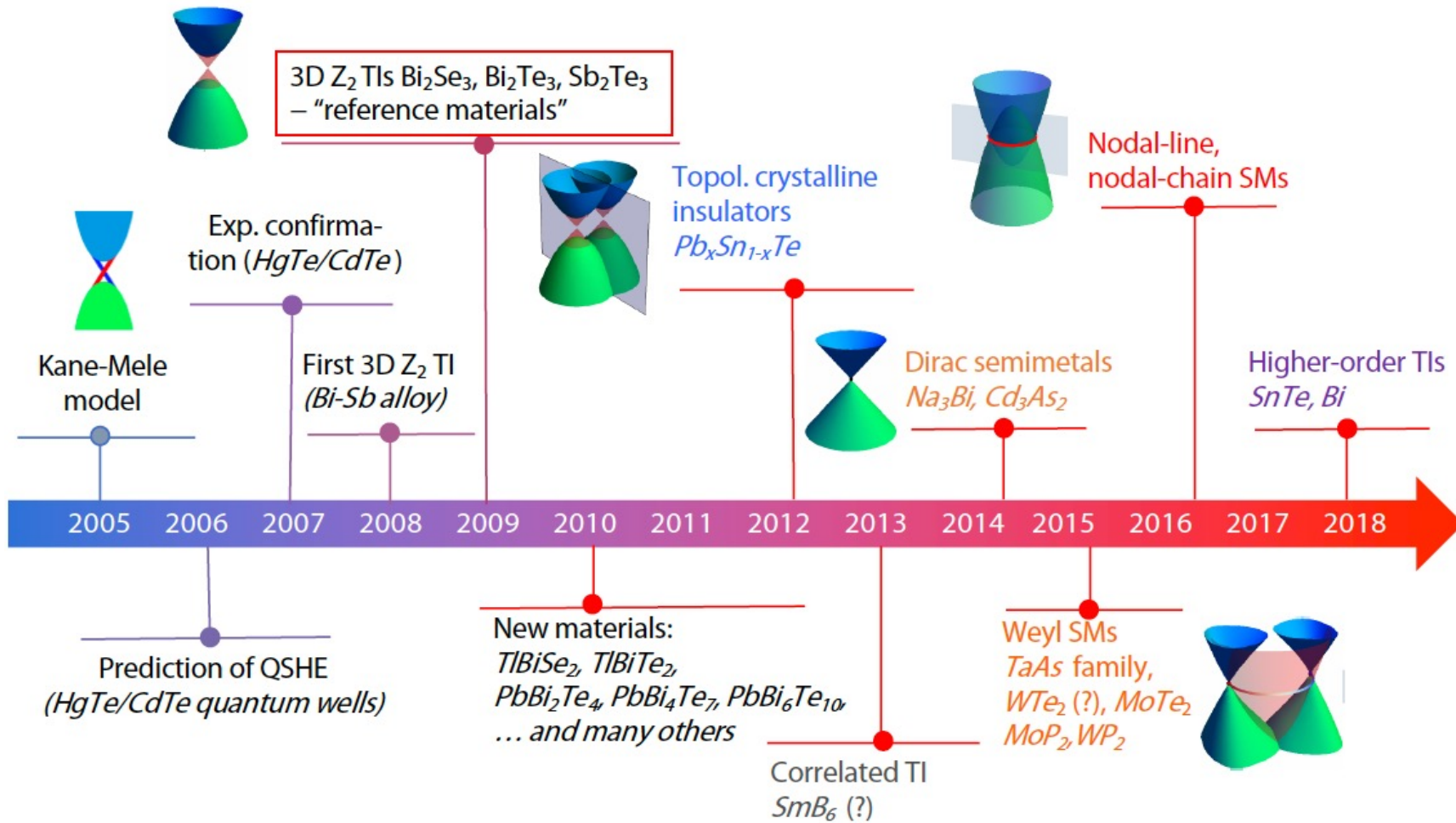
Electronic structure of Bi chalcogenides

- band inversion results from competing spin-orbit and ligand/crystal field splitting
- spin-orbit coupling is inherited from atoms
- spin-orbit coupling defines the band gap
- a simple model provides quantitative description

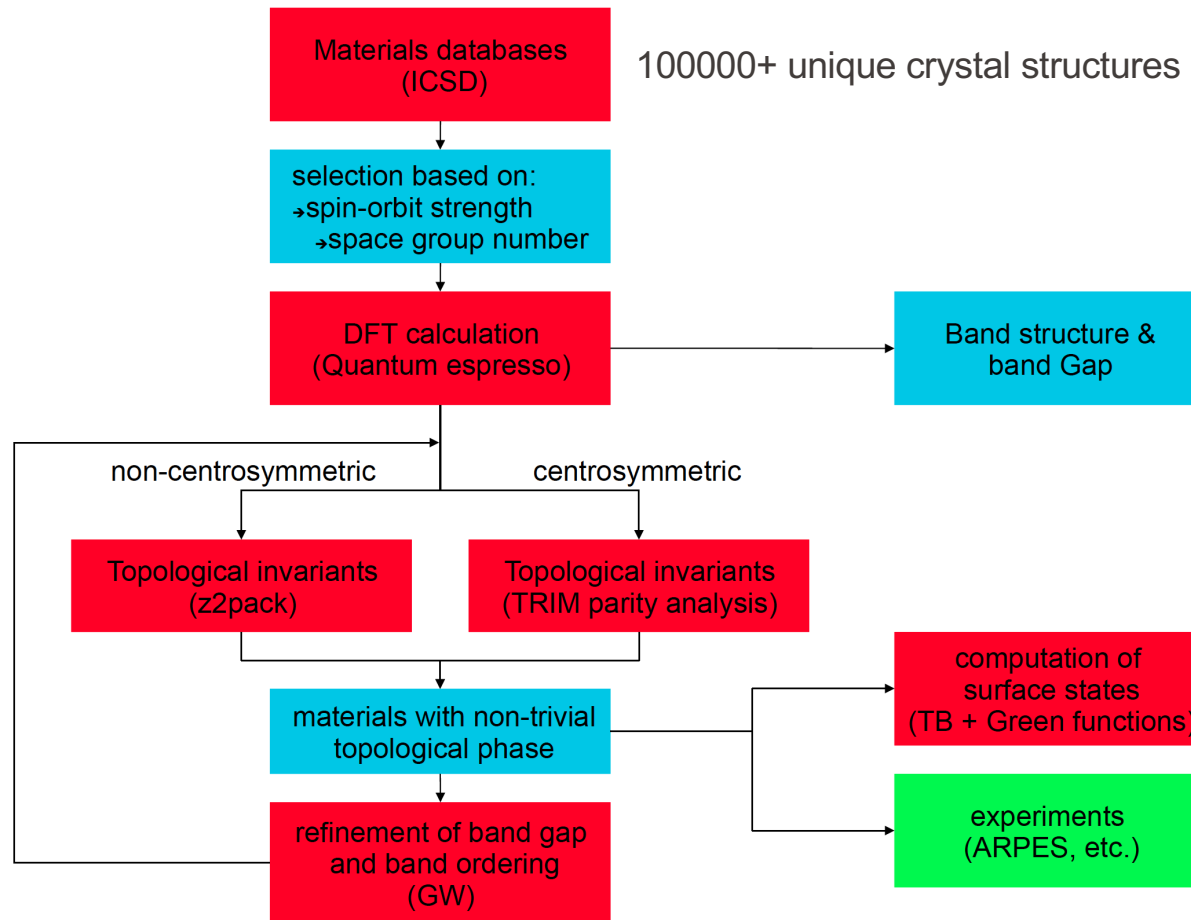
Bi₂Se₃



Timeline of the field of topological materials



High-throughput search protocol



G. Autès (C3MP)



NCCR Marvel

European Research Council



ERC Starting grant TopoMat

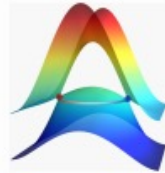
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TopoMat database @ Materials Cloud

- started in 2013, made publicly available in 2018
- crystal structures from ICSD and COD databases (experimental XRD data) – total 108423 unique crystal structures
- currently 13628 entries (“pre-screened” materials: <20 atoms per unit cell, even number of electrons, no lanthanides)
- band structures, Z_2 indices, Wannier charge center plots (Z2Pack), etc.
- >4000 materials with nontrivial Z_2 indices
- all data is freely available on Materials Cloud

doi: 10.24435/materialscloud:2019.0019/v2



TopoMat: a database of high-throughput first-principles calculations of topological materials

DOI [10.24435/materialscloud:2019.0019/v1](https://doi.org/10.24435/materialscloud:2019.0019/v1)

Authors: Gabriel Autès, QuanSheng Wu, Nicolas Mounet & Oleg V. Yazyev

Description: The database contains the results of high-throughput first-principles screening of known crystal structures for topological materials (topological insulators, Dirac and Weyl semimetals, etc.). If you use this work please cite the following publication in progress: G. Autès, Q. S. Wu, N. Mounet & O. V. Yazyev, “TopoMat: a database of high-throughput first-principles calculations of topological materials”, in preparation (2018).

TopoMat database @ Materials Cloud

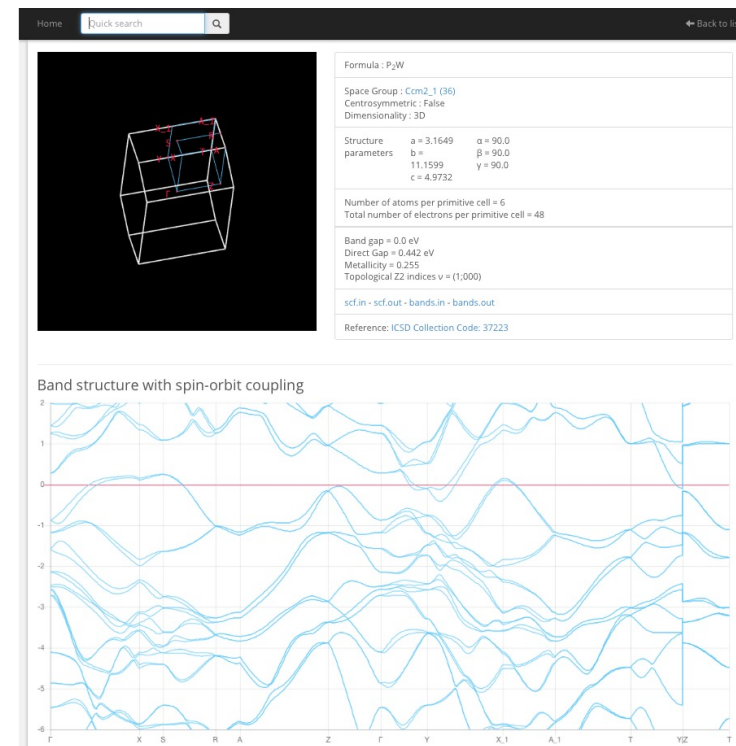
- web interface and search engine on Materials Cloud
<https://www.materialscloud.org/discover/topomat>

Home Quick search X-axis Y-axis Plot

Space Group: 166 Centro. Non Centro. All
 1D 2D 3D All
 Composition Bi₂Se₃ (V₀V₁V₂V₃) (1,000) Source ID 165226 Non-trivial only

13628 materials founds

Formula	Source	ID	space group	centered	nat	ne	dim	gap	dir. gap	met.	v	wcc	updated
Ag	COD	1509145	P6 ₃ /mmc (194)	✓	2	22	3	0.0	0.000	0.772	(0,000)	x	05/01/17
Ag	COD	1509194	P6 ₃ /mmc (194)	✓	4	44	3	0.0	0.004	0.873	(1,000)	x	05/01/17
Ag ₂ BiO ₃	COD	1509762	Pnna (52)	✓	24	220	3	0.0	0.017	0.038	(1,011)	x	07/08/17
Ag ₂ CN ₂	ICSD	411091	P2 ₁ /c (14)	✓	20	144	3	1.1872	1.187	0.000	(0,000)	x	02/02/17
Ag ₂ CO ₃	COD	1007035	P2 ₁ /m (11)	✓	12	88	3	0.6496	1.356	0.000	(0,000)	x	27/01/17
Ag ₂ GeS ₃	ICSD	41711	Cmc2 ₁ (36)	x	12	88	3	0.1033	0.103	0.000	(0,000)	✓	28/11/16
Ag ₂ H ₂ IOF	ICSD	32660	P2 ₁ (4)	x	14	88	3	1.2016	1.282	0.000	(0,000)	x	16/03/17
Ag ₂ Hg ₄	ICSD	25592	I-4 (82)	x	7	62	3	1.0077	1.008	0.000	(0,000)	x	06/10/16
Ag ₂ Hg ₄	ICSD	30264	P-42m (111)	x	7	62	3	0.8694	0.869	0.000	(0,000)	x	07/10/16
Ag ₂ Hg ₄	ICSD	6069	I-4 (82)	x	7	62	3	1.0269	1.027	0.000	(0,000)	x	06/10/16
Ag ₂ Hg ₄	ICSD	150343	I-4 (82)	x	7	62	3	1.0055	1.006	0.000	(0,000)	x	06/10/16
Ag ₂ HgO ₂	COD	7109248	P4 ₃ 2 ₁ 2 (96)	x	20	184	3	0.581	0.581	0.000	(0,000)	x	16/03/17
Ag ₂ HgS ₂	COD	9009717	P2 ₁ /c (14)	✓	10	92	3	0.5114	0.511	0.000	(0,000)	x	30/01/17
Ag ₂ HgSi ₂	ICSD	413300	Cmc2 ₁ (36)	x	12	108	3	1.0911	1.122	0.000	(0,000)	x	16/03/17
Ag ₂ Mo ₂ O ₇	COD	4027813	P-1 (2)	✓	22	184	3	1.8258	1.847	0.000	(0,000)	x	07/08/17

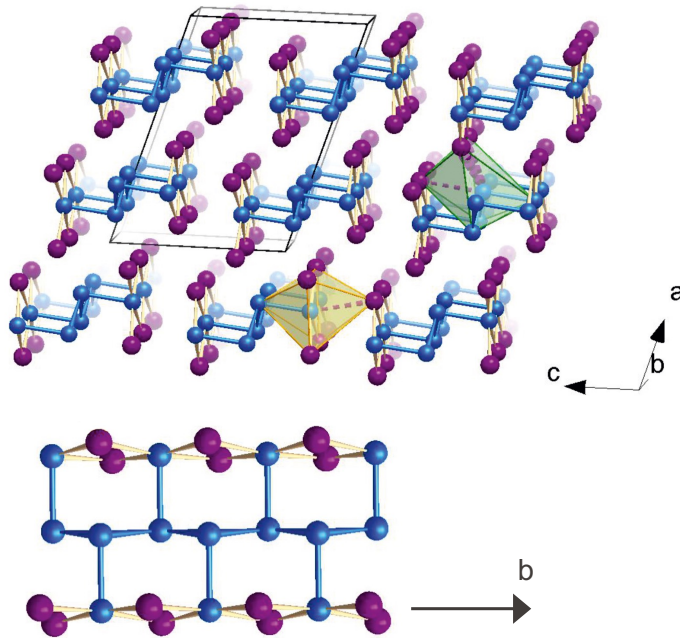


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β -Bi₄I₄ – a «candidate» topological insulator

- quasi-1D crystal structure (space group C12/m1)

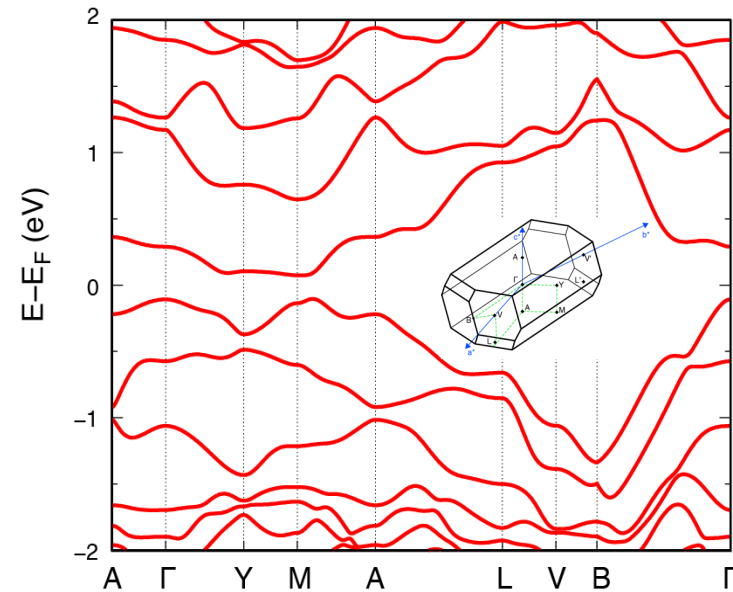


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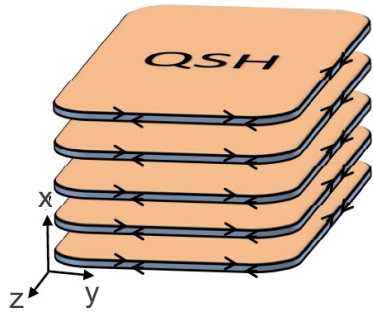
Urazov & Sokolova, 1954
von Schnering *et al.*, 1978

- DFT predictions
 - band gap 0.14 eV
 - «weak» TI (0;001)
 - band inversion at points M and Y

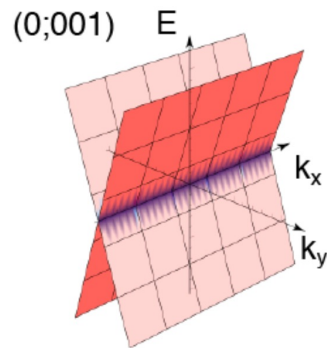


β -Bi₄I₄ – signatures of the topological phase

- weak 3D TI = stack of 2D TIs

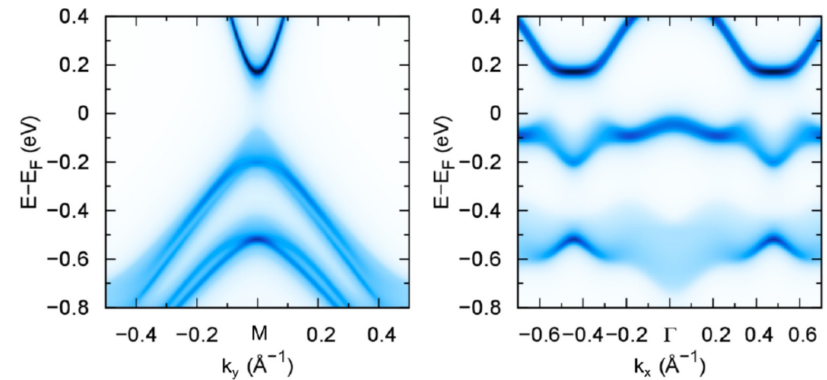


- surface-state dispersion at side surfaces = Dirac “groove”

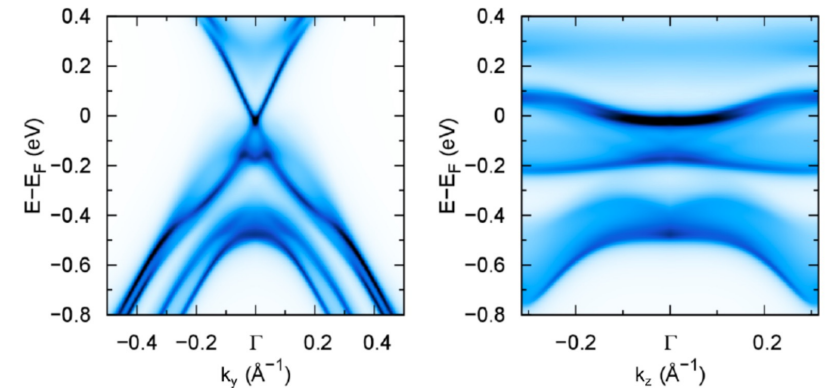


- Predicted dispersion:

- (001) surface



- (100) surface



β -Bi₄I₄ – synthesis and characterization

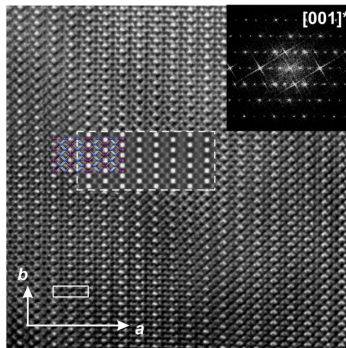
■ synthesis



A. Isaeva (TU Dresden)

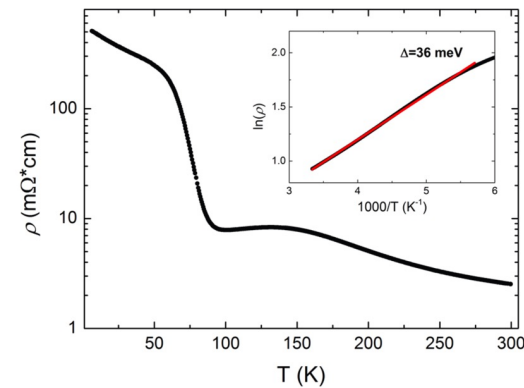


■ TEM characterization



W. van den Broek
(Ulm)

■ transport measurements



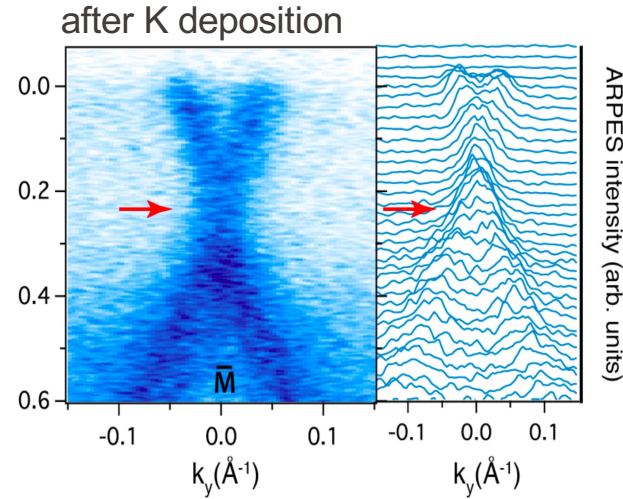
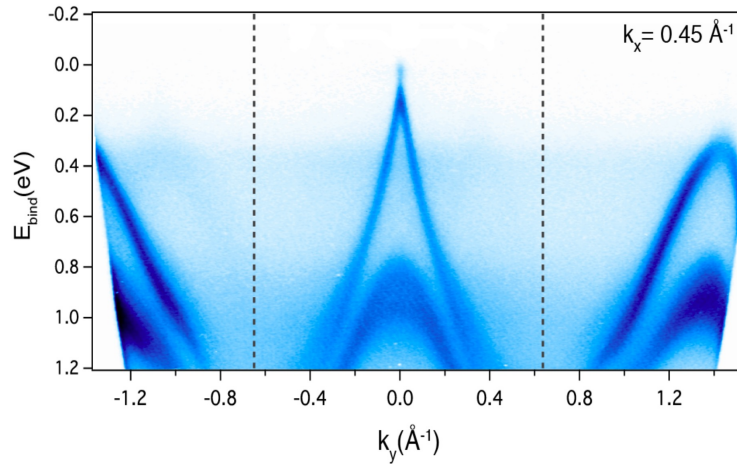
A. Pisoni, L. Forro
(EPFL)

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β -Bi₄I₄ – ARPES measurements

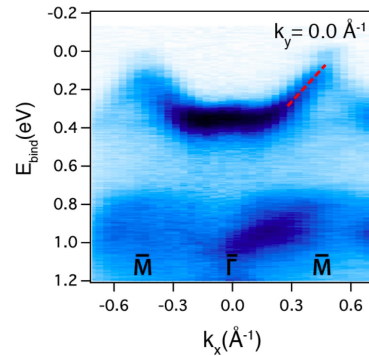
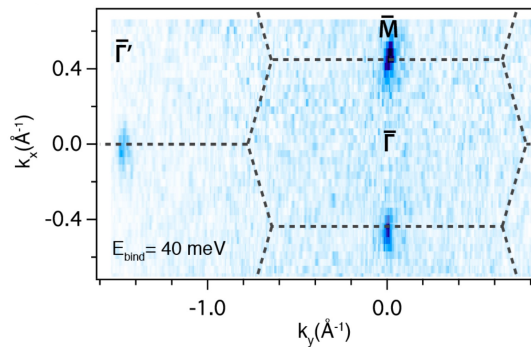
- A clean band crossing



L. Moreschini (ALS)

J. Johannsen (EPFL)
M. Gioni (EPFL)

- ... but at (001) surface, and anisotropic Dirac cone



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First-principles calculations (DFT vs. MBPT)

■ Density functional theory (DFT)

- Kohn-Sham formalism

$$\left[-\frac{1}{2} \nabla^2 + V_{\text{ion}} + V_{\text{H}} + V_{\text{xc}}^{\text{DFT}} \right] \psi_{n\mathbf{k}}^{\text{DFT}} = E_{n\mathbf{k}}^{\text{DFT}} \psi_{n\mathbf{k}}^{\text{DFT}}$$

Hohenberg & Kohn '64
Kohn & Sham '65

- Good for: ground-state properties (structural, cohesive, vibrational, magnetic, ...)
- Bad for: excited-state properties (photoemission, band gaps, band offsets, optical, ...)

■ Many-body perturbation theory (MBPT)

- GW formalism: Green's function approach + quasiparticle approximation

$$\left[-\frac{1}{2} \nabla^2 + V_{\text{ion}} + V_{\text{H}} + \underline{\Sigma(E_{n\mathbf{k}}^{\text{QP}})} \right] \psi_{n\mathbf{k}}^{\text{QP}} = \underline{E_{n\mathbf{k}}^{\text{QP}}} \psi_{n\mathbf{k}}^{\text{QP}}$$

$\Sigma = iGW$ - self energy

G - one-particle Green's function

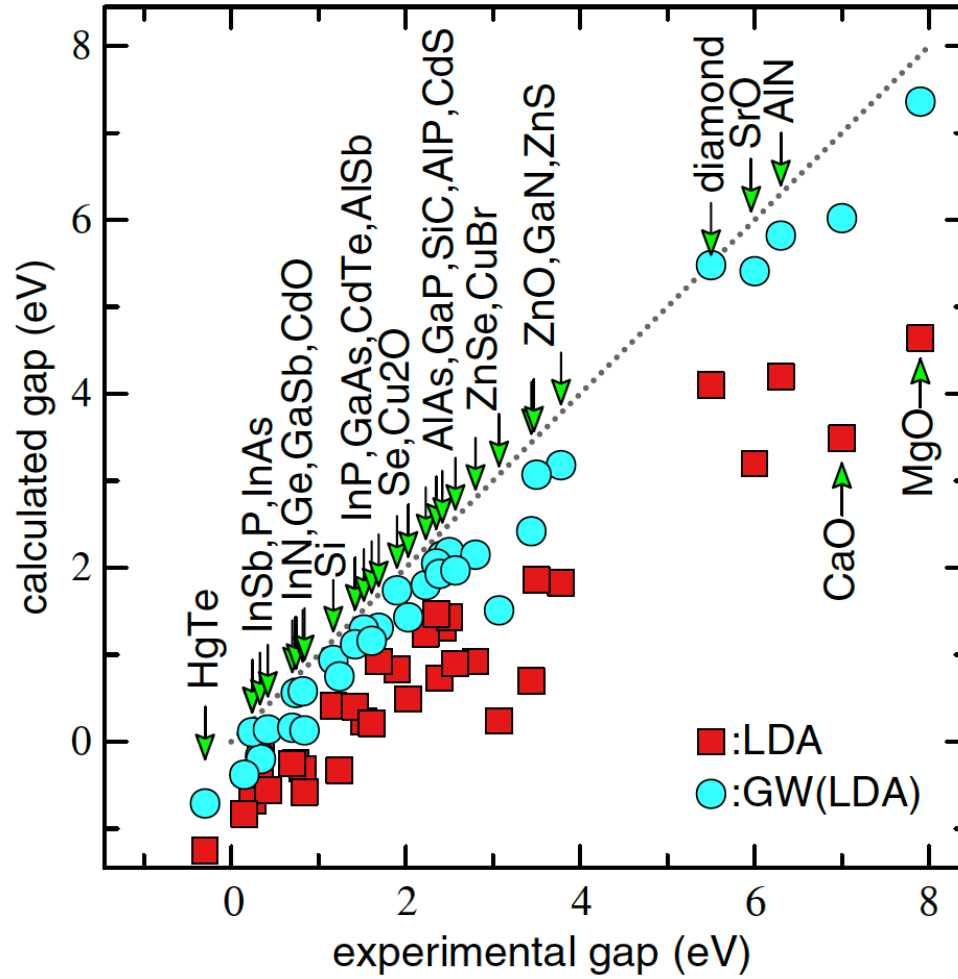
$W = \varepsilon^{-1}v$ - screened Coulomb interaction



Hedin '65
Hybertsen & Louie '85

The band-gap problem

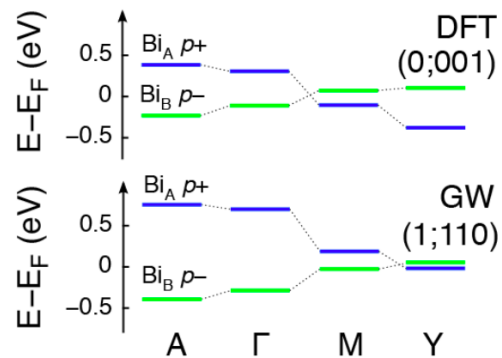
- DFT vs. GW results



From van Schilfgaarde *et al.*,
 Phys. Rev. Lett. **96**, 226402 (2006)

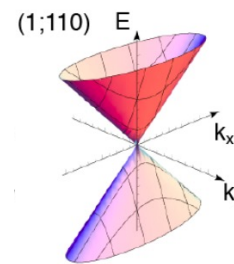
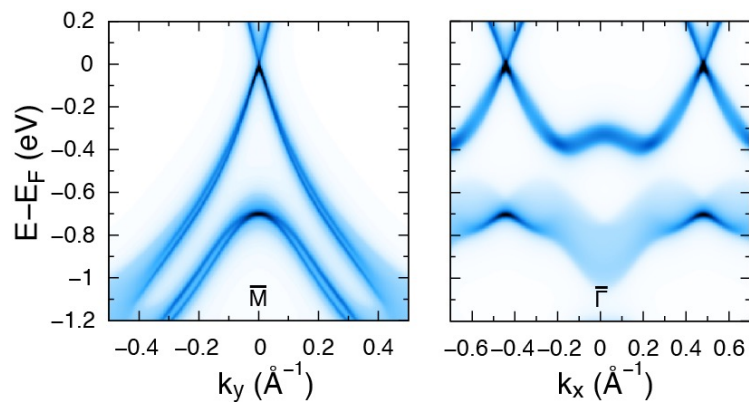
β -Bi₄I₄: the «revised» predictions (GW)

- DFT “exaggerates” band inversion (Yazyev *et al.*, PRB’12)
- GW corrections eliminate band inversion at point M



- “weak” topological insulator (0;001)
- “strong” topological insulator (1;110)
- band gap 0.037 eV

■ Simulated ARPES at the (001) surface

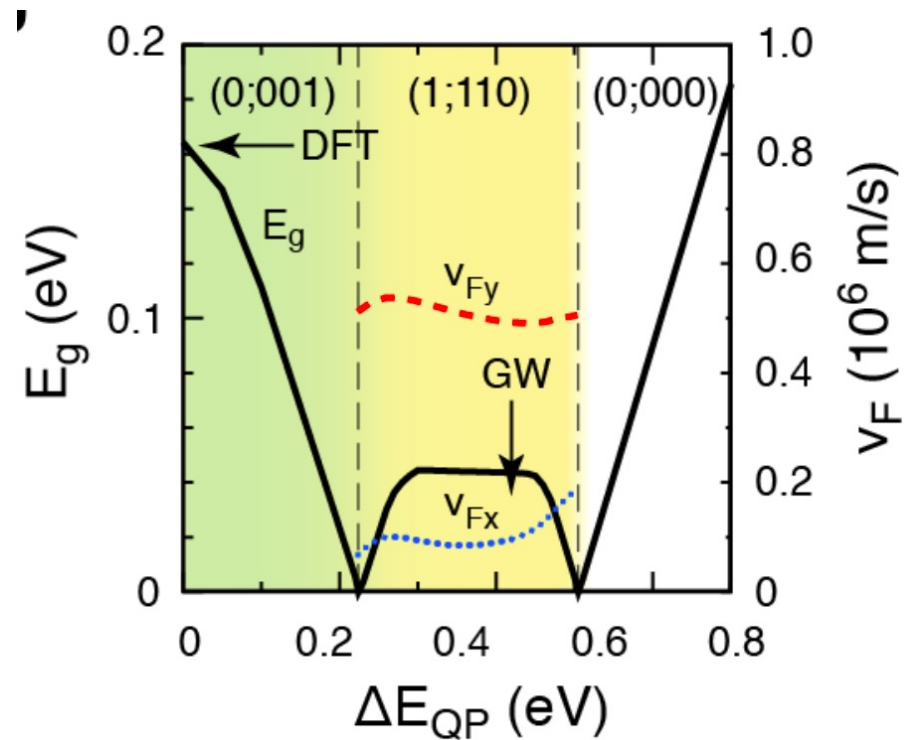


anisotropic Dirac fermions

G. Autès *et al.*, Nature Materials **15**, 154 (2016)

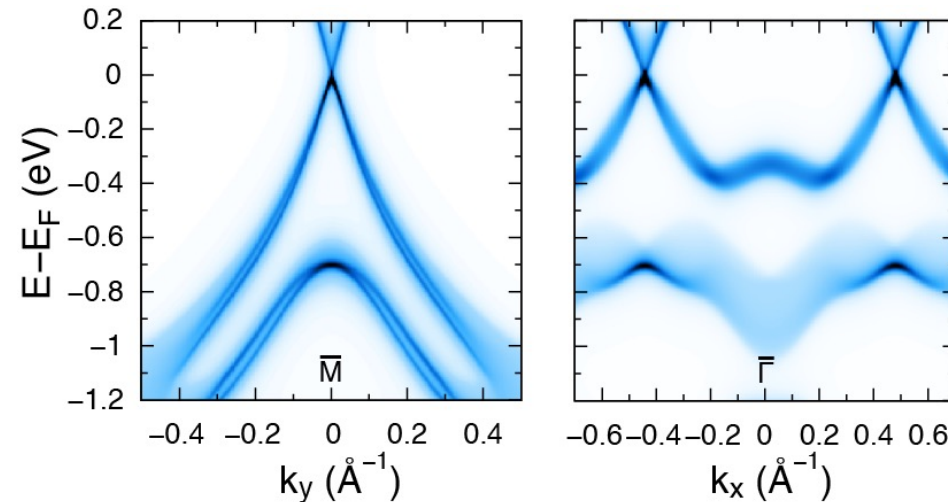
β -Bi₄I₄: possible phases

- Rigid quasiparticle shift before introducing spin-orbit interactions

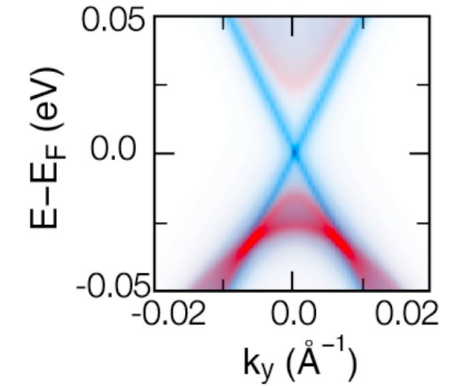


β -Bi₄I₄ : theory vs. experiment

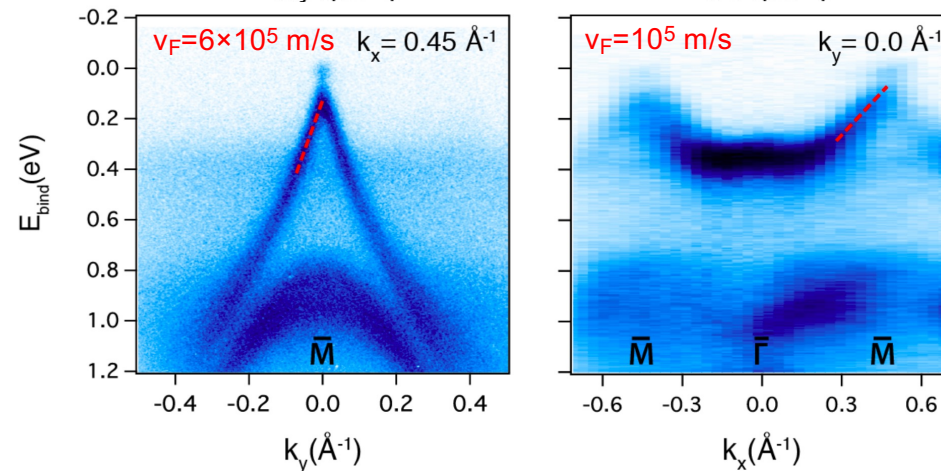
- Theory (GW)



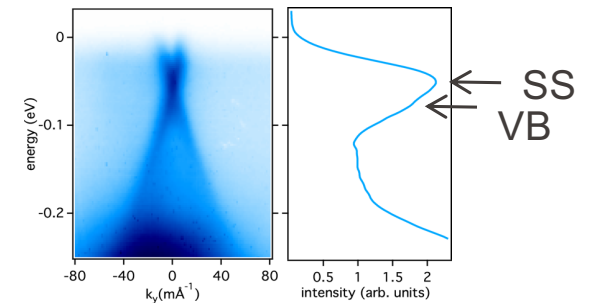
- close view (bulk/surface)



- Experiment



- 6 eV laser ARPES



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G. Autès *et al.*, Nature Materials **15**, 154 (2016)

β -Bi₄I₄: theory + experiment

- Full cycle of material discovery = prediction, synthesis, characterization, confirmation

LETTERS

PUBLISHED ONLINE: 14 DECEMBER 2015 | DOI: 10.1038/NMAT4488

nature
materials

A novel quasi-one-dimensional topological insulator in bismuth iodide β -Bi₄I₄

Gabriel Autès^{1,2†}, Anna Isaeva^{3†}, Luca Moreschini^{4†}, Jens C. Johansen^{5†}, Andrea Pisoni⁵, Ryo Mori^{6,7}, Wentao Zhang^{6,8}, Taisia G. Filatova⁹, Alexey N. Kuznetsov⁹, László Forró⁵, Wouter Van den Broek¹⁰, Yeongkwan Kim^{4,11}, Keun Su Kim^{12,13}, Alessandra Lanzara^{6,8}, Jonathan D. Denlinger⁴, Eli Rotenberg⁴, Aaron Bostwick⁴, Marco Grioni⁵ and Oleg V. Yazyev^{1,2*}

■ - theory (Lausanne)

■ - materials synthesis (Dresden, Moscow)

■ - synchrotron ARPES (Berkeley, Lausanne, Seoul)

■ - 6 eV laser ARPES (Berkeley)

■ - transport characterization (Lausanne)

■ - TEM characterization (Ulm)

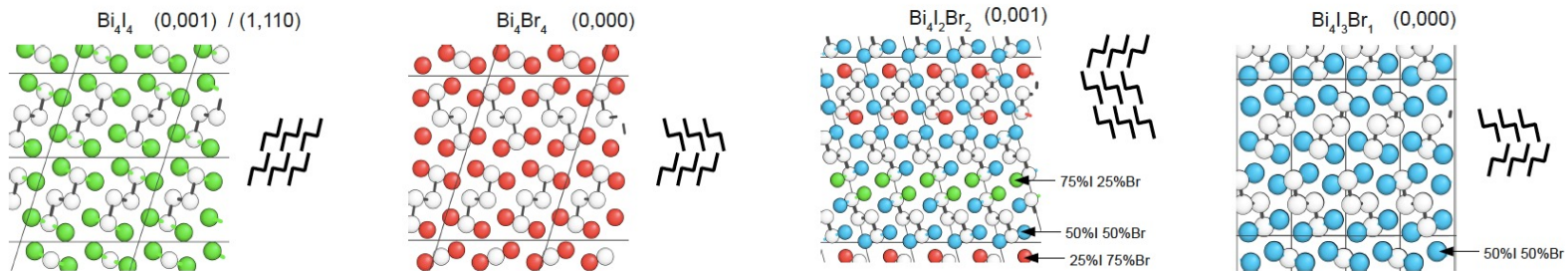
- C3MP

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G. Autès *et al.*, Nature Materials **15**, 154 (2016)

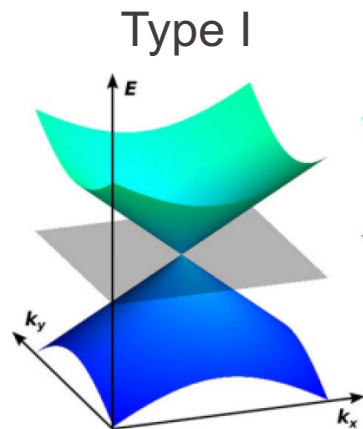
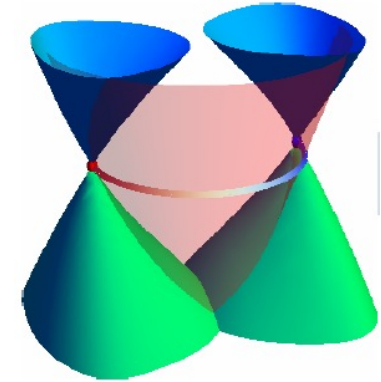
β -Bi₄I₄: conclusions and outlook

- β -Bi₄I₄ is a new strong TI, very different from other known TIs
- quasi-1D structure and anisotropic Dirac fermion surface states
- very few defects and low concentration of intrinsic charge carriers
- close to the topological phase transitions to the “weak” TI (0;001) and trivial (0;000) phases, “weak” TI claimed by some groups recently
- opens an entirely new class of Bi halide topological materials (ongoing)
- higher-order topological and QSH (in thin films) insulators found by other groups



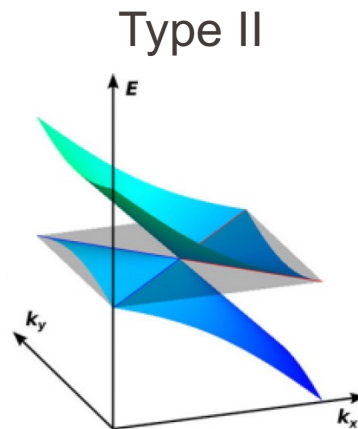
Weyl semimetals

- chiral point degeneracies (Weyl fermions)
- required breaking inversion or time-reversal symmetry
- Fermi arc surface states
- anomalous magnetotransport (chiral anomaly)



TaAs, NbAs, TaP, NbP

Lv *et al.*, 2015



WTe₂ (?), MoTe₂

A. Soluyanov *et al.*, Nature 527, 495 (2015)



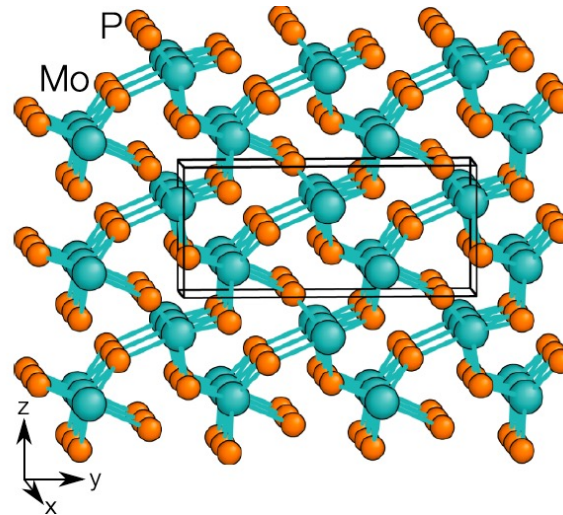
A. Soluyanov

1982 – 2019

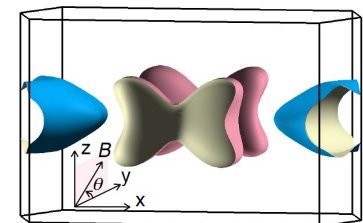
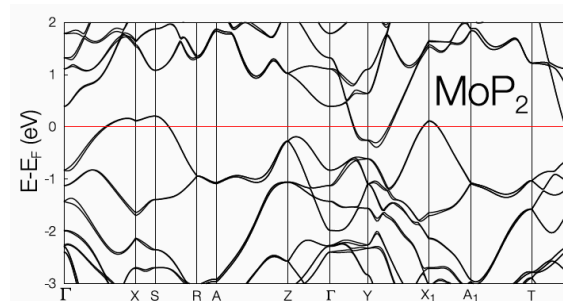
Candidate Weyl semimetals MoP_2 and WP_2

- base-centered orthorhombic crystal structure
- space group $\text{Cmc}2_1$ (No. 36)
- symmetries:
 - C_2 screw axis along $[001]$
 - mirror plane (010)
 - glide plane (100)

- compensated semimetals
- very similar band structures



Rundqvist and Lundström '63
Rühl and Jeitschko '83

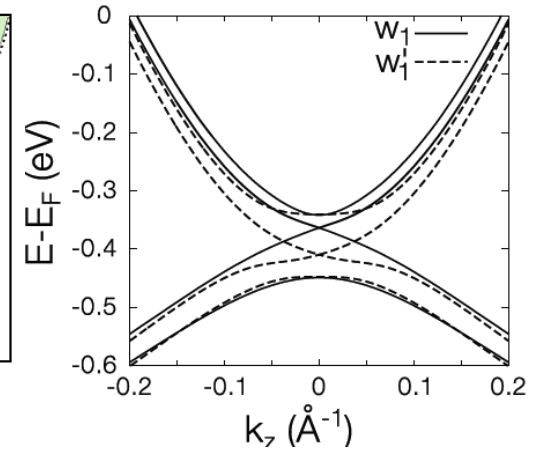
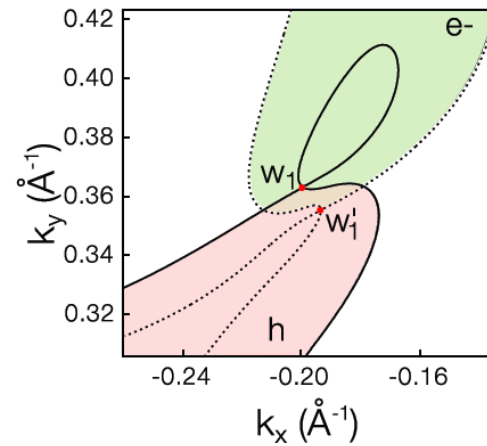
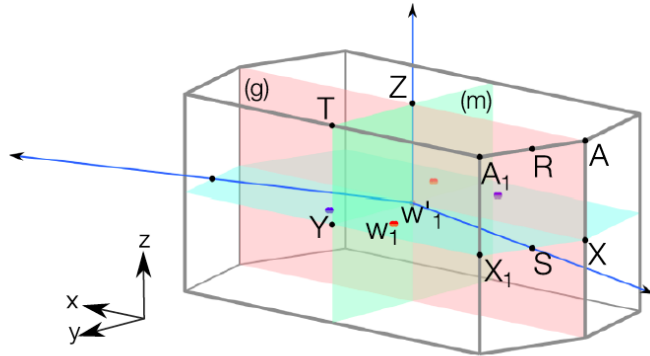


Fermi surface

Autès *et al.*, Phys. Rev. Lett. **117**, 066402 (2016)

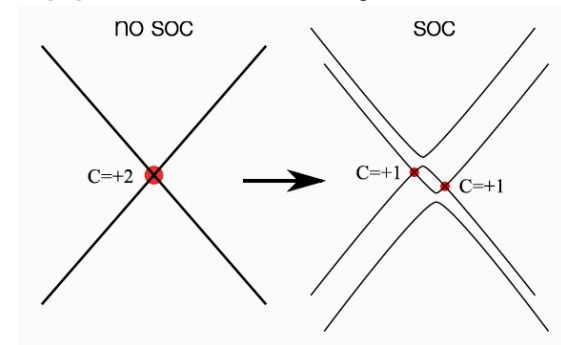
Candidate Weyl semimetals MoP₂ and WP₂

- 8 Weyl points of type II in $k_z = 0$ plane



- Robust Weyl semimetal phase
 - large distance in k space between Weyl points of opposite chirality

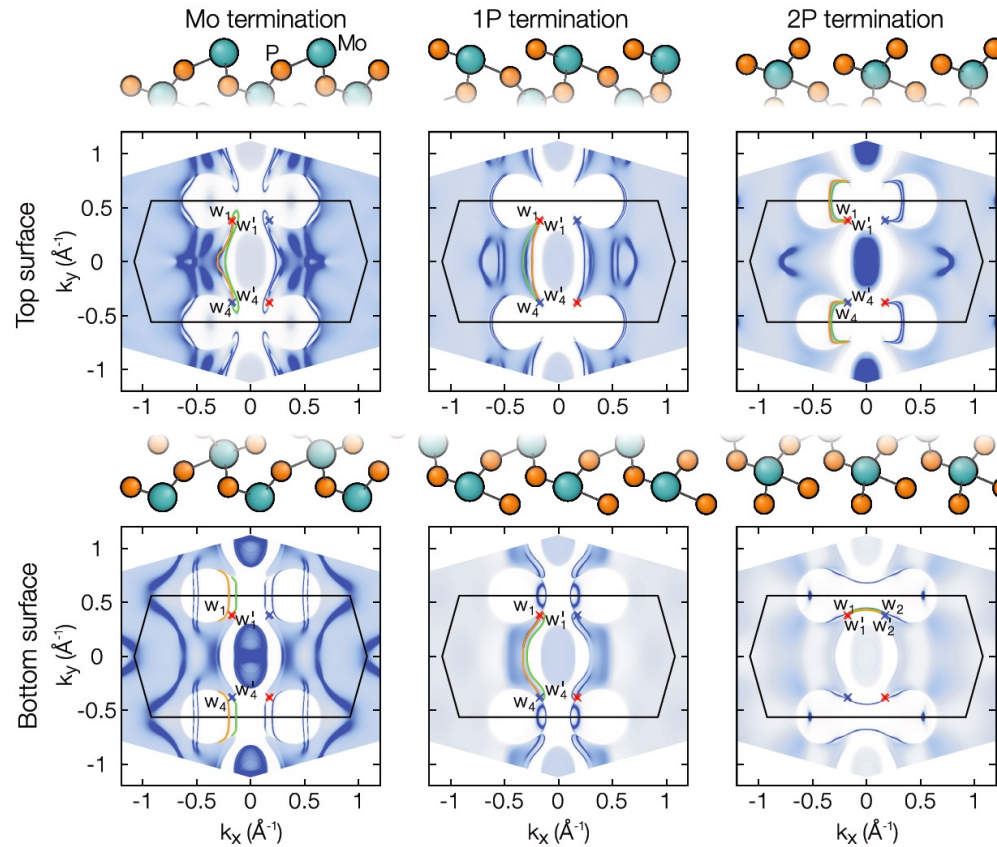
TaAs family: ~4% of reciprocal lattice vector;
 WTe₂ family ~1%
 MoP₂ and WP₂ ~**25%**



Autès *et al.*, Phys. Rev. Lett. **117**, 066402 (2016)

Candidate Weyl semimetals MoP_2 and WP_2

- Long Fermi arcs that depend on surface termination



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Autès *et al.*, Phys. Rev. Lett. **117**, 066402 (2016)

Early experimental results

- very high low-T conductivity ($\rho \approx 3 \text{ n}\Omega \text{ cm}$ at 2 K)
- residual resistivity ratios (RRR ≈ 25000) record for binary materials
- highest measured magnetoresistances ($2 \times 10^8 \%$ at 63 T and 0.5 K, $4 \times 10^6 \%$ at 9 T and 2 K)
- mean free path of **0.5 mm**

N. Kumar *et al.*, Nat. Commun. 8, 1642 (2017)

- **hydrodynamic electron fluid** transport below 20 K

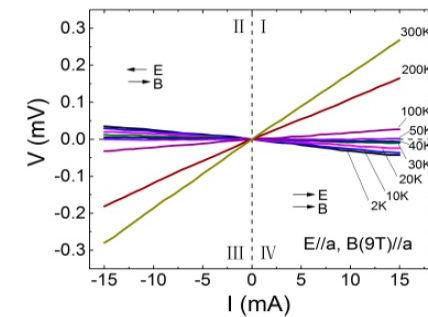
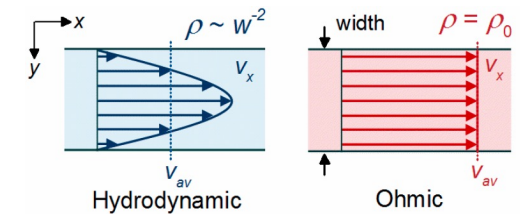
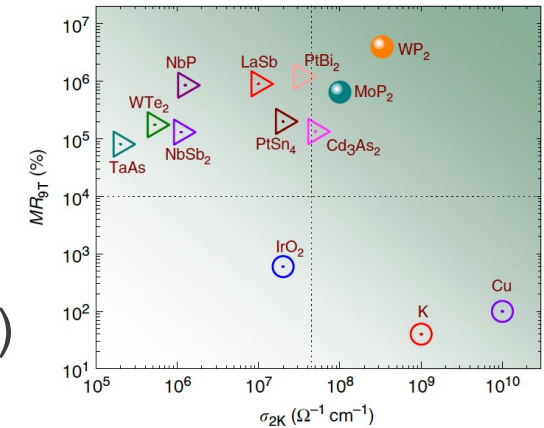
J. Gooth *et al.*, Nat. Commun. 9, 4093 (2018)

- **“negative” resistivity** (at low T and for $B \parallel E$)

Y.-Y. Lv *et al.*, arXiv:1708.03489

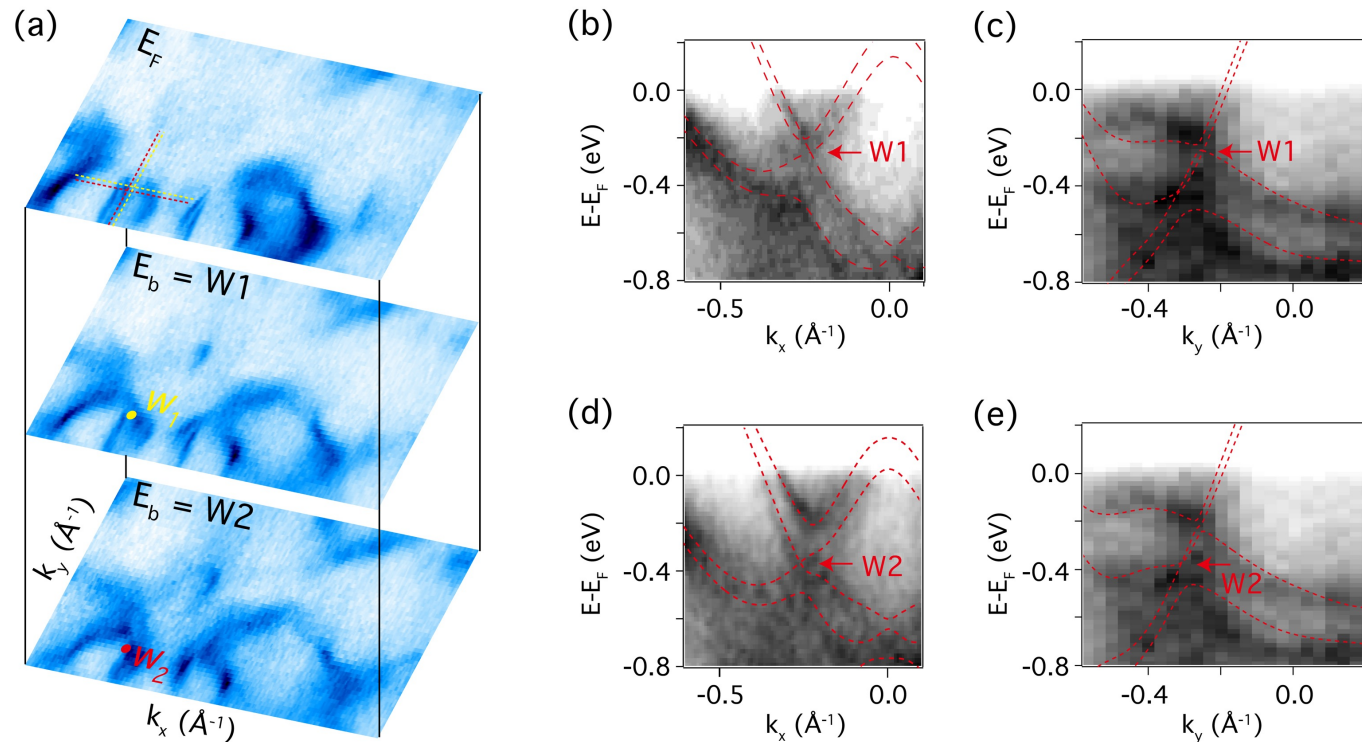
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ARPES confirmation of Weyl nodes in WP_2

- Very good agreement with DFT calculations

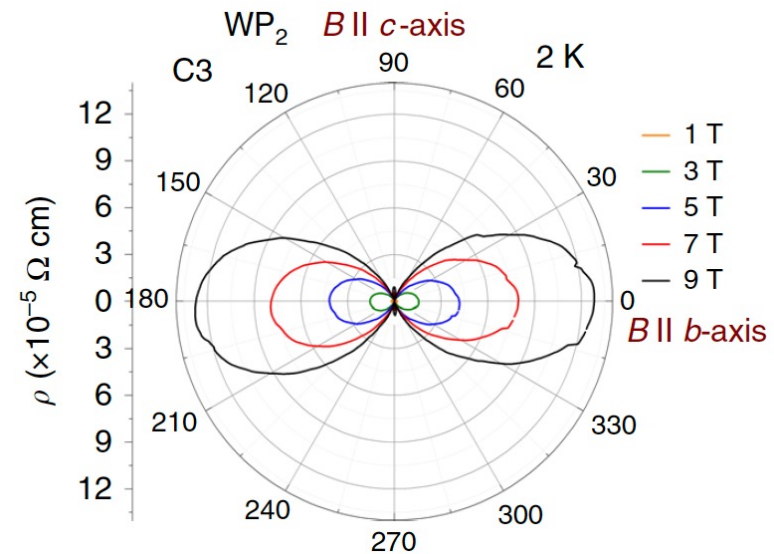
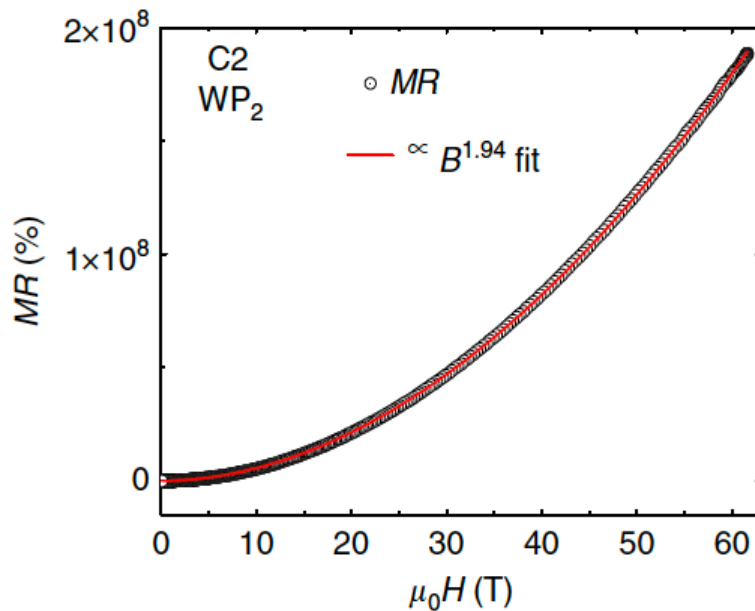


ARPES:
group M. Shi (PSI)

Transverse magnetoresistance in WP_2

Magnetoresistance $MR(B) = \frac{\rho(B) - \rho(0)}{\rho(0)}$

- Extremely large, non-saturating, nearly quadratic MR ($I \parallel a$, $B \parallel b$)
- No sign of quantum oscillations
- Very pronounced MR anisotropy

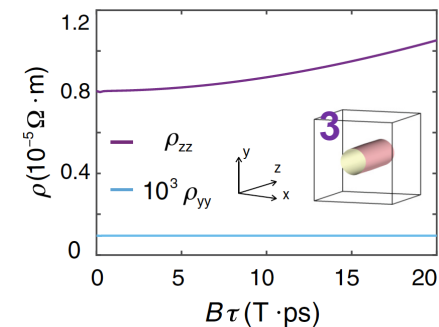
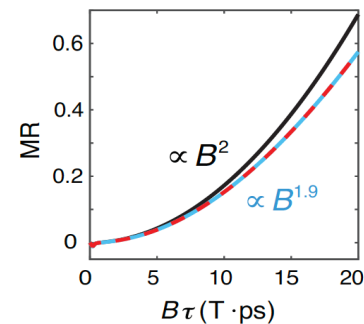
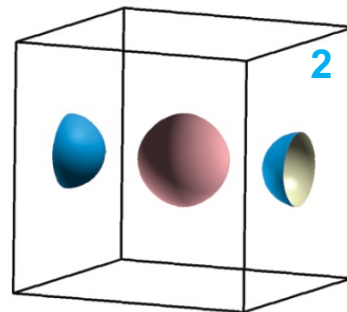
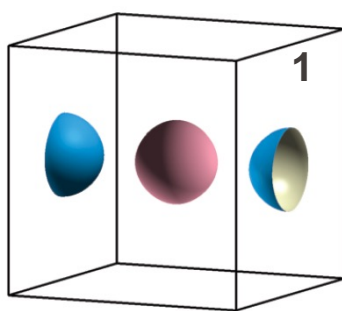
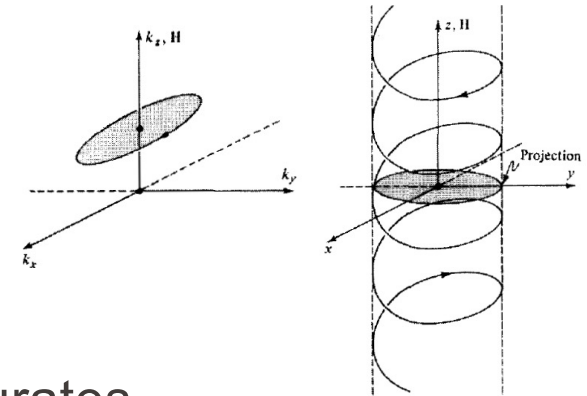


N. Kumar *et al.*, Nat. Commun. 8, 1642 (2017)

Origin of non-saturating MR

Within the semiclassical approximation:

- free electrons (spherical Fermi surface) : $MR = 0$
- nearly free electrons : $MR \propto B^2$, then saturates
- compensated semimetal (1) : $MR \propto B^2$, never saturates
- nearly compensated semimetal (2) : $MR \propto B^n$, $n < 2$
- open orbits (3) : non-saturating for current along the open direction



MR within semiclassical approximation

- Boltzmann transport approach

$$\sigma_{ij}^{(n)}(\mathbf{B}) = \frac{e^2}{4\pi^3} \int d\mathbf{k} \tau_n \mathbf{v}(\mathbf{k}) \bar{\mathbf{v}}(\mathbf{k}) \left(-\frac{\partial f}{\partial \varepsilon} \right)_{\varepsilon=\varepsilon_n(\mathbf{k})}$$

$$\mathbf{v}_n(\mathbf{k}) = \frac{1}{\hbar} \nabla_{\mathbf{k}} \varepsilon_n(\mathbf{k}) \quad \frac{d\mathbf{k}_n(t)}{dt} = -\frac{e}{\hbar} \mathbf{v}_n[\mathbf{k}(t)] \times \mathbf{B}$$

$$\bar{\mathbf{v}}_n(\mathbf{k}) = \int_{-\infty}^0 \frac{dt}{\tau_n} e^{\frac{t}{\tau_n}} \mathbf{v}_n[\mathbf{k}(t)]$$

S.N. Zhang, Q.S. Wu, Y. Liu, O. V. Yazyev, PRB 99, 035142 (2019)

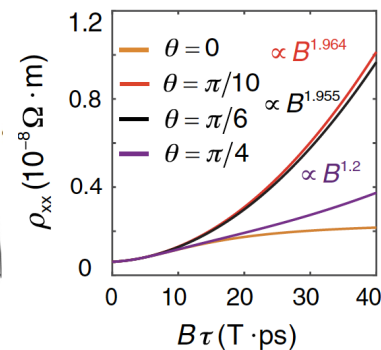
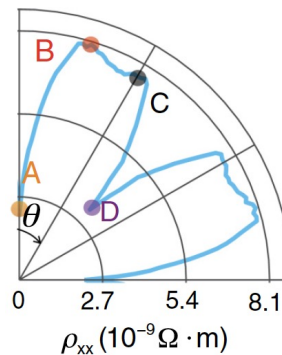
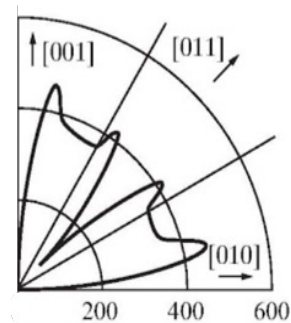
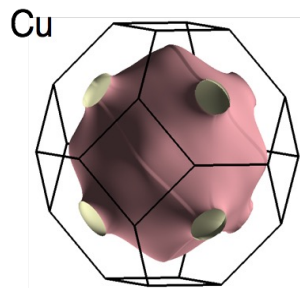


S.N. Zhang
implemented in WannierTools code



Q.S. Wu

- Combined with first-principles calculations and Wannier function techniques
- Typically, compares well to experiments, even in constant τ approximation



- A: free electron like, some compensation
- B: open orbits
- C: open orbits
- D: complex (compensation + open orbits)

Exp.: Klaunder and Kunzler, *The Fermi Surface* (1960)

MR in WP_2 from theory perspective

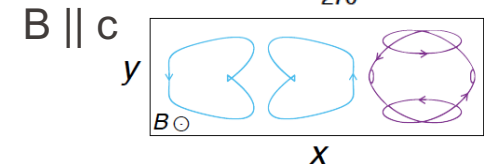
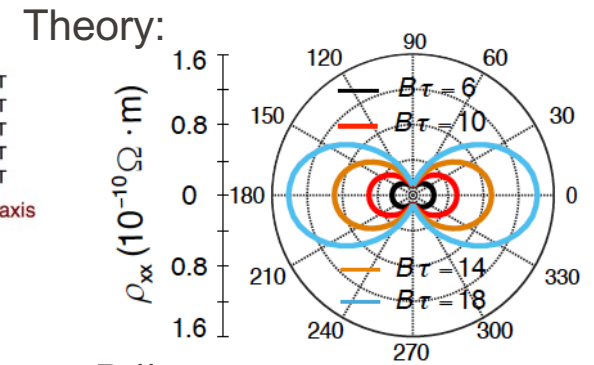
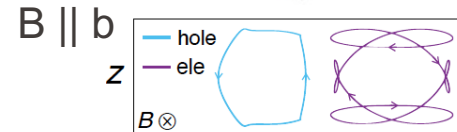
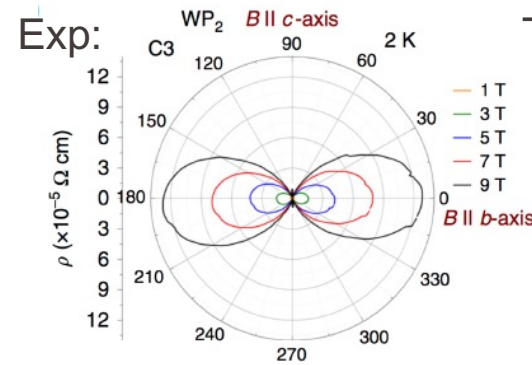
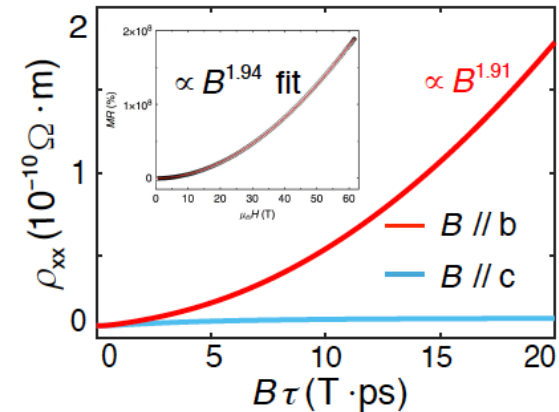
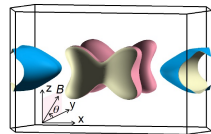
- non-saturating MR results from ordinary charge carrier compensation
- not directly related to the Weyl semimetal phase, but implies a relatively long $\tau = 10^{-9}$ s
- novel mechanism for strong MR anisotropy
 - for $B \parallel c$, hole carriers follow elec. orbits
 - result of concave FS segments

N.P. Ong, PRB 43, 193 (1991)

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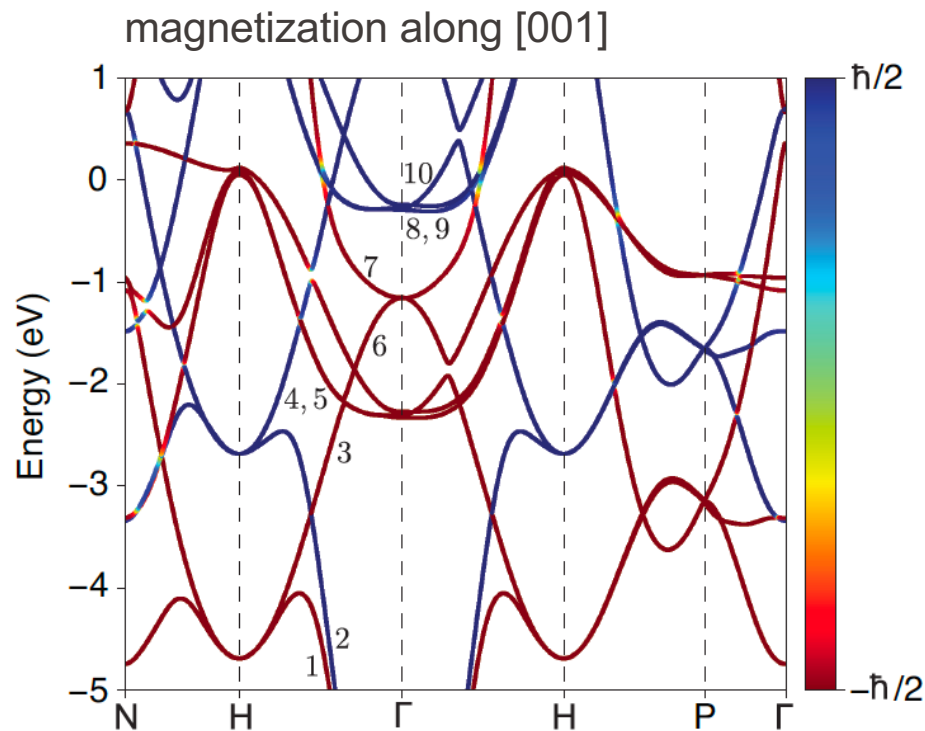
Fermi surface of WP_2



S.N. Zhang, Q.S. Wu, Y. Liu, O. V. Yazyev, PRB 99, 035142 (2019)

Band structure of ordinary bcc iron

- Numerous Weyl points across the band structure as a result of broken time-reversal symmetry



bands 6 and 7

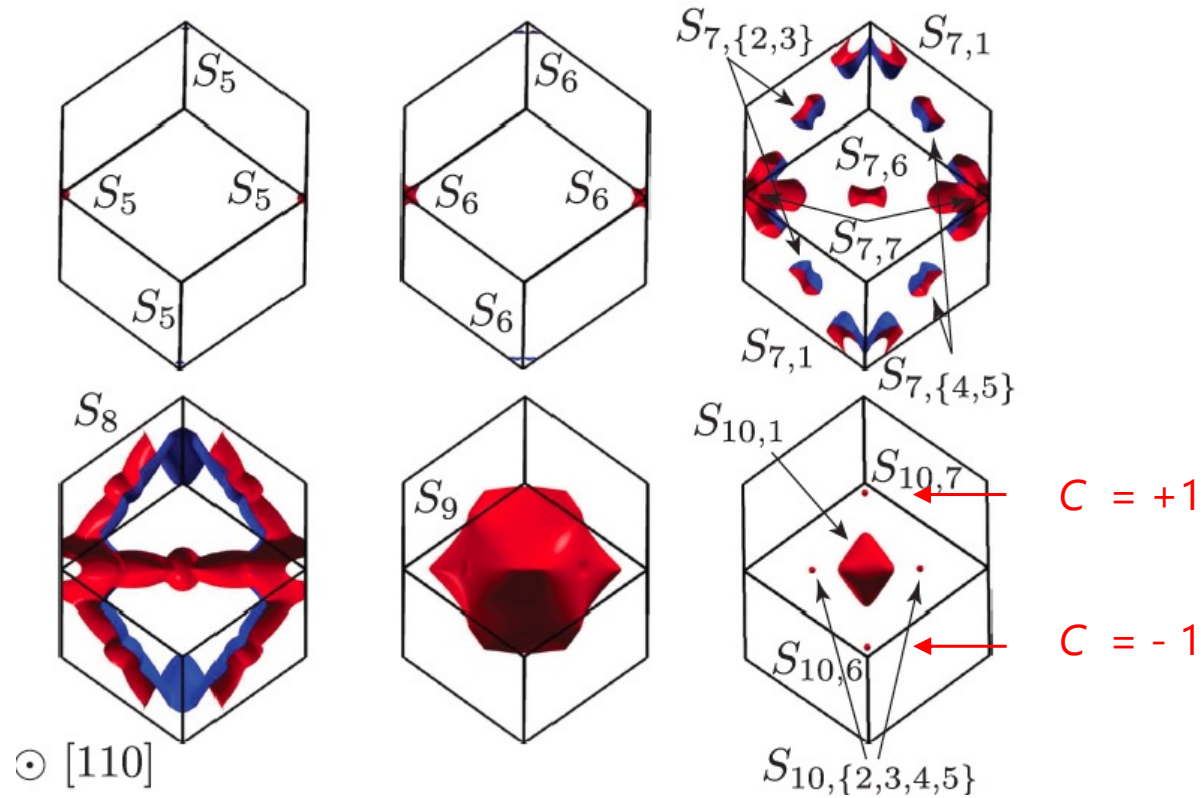
k_x	k_y	k_z	Proj.	E	Spin	χ	Mult.
0.0	0.0	0.027	$\bar{\Gamma}$	-1.16	$\downarrow\downarrow$	-2	1
0.0	1.0	0.056	\bar{M}	0.06	$\downarrow\downarrow$	-1	1
0.5	0.5	0.130	\bar{X}	-0.96	$\downarrow\downarrow$	+1	2
0.180	0.820	0.180	$\bar{X}\bar{M}$	-0.34	$\sim\downarrow\downarrow$	+1	4
0.074	0.322	0.242	gen.	-1.01	$\uparrow\downarrow$	-1	8
0.0	0.327	0.243	$\bar{\Gamma}\bar{M}$	-0.99	$\uparrow\downarrow$	+1	4
0.0	0.583	0.284	$\bar{\Gamma}\bar{M}$	-0.87	$\downarrow\downarrow$	+1	4
0.0	0.217	0.316	$\bar{\Gamma}\bar{M}$	-0.99	$\uparrow\uparrow$	+1	4
0.135	0.662	0.338	gen.	-1.07	$\downarrow\downarrow$	-1	8
0.0	0.365	0.365	$\bar{\Gamma}\bar{M}$	-1.02	$\uparrow\uparrow$	-1	4
0.118	0.118	0.429	$\bar{\Gamma}\bar{X}$	-0.84	$\uparrow\downarrow$	-1	4
0.0	1.0	0.446	\bar{M}	-0.94	$\uparrow\downarrow$	+1	1

bands 9 and 10

k_x	k_y	k_z	Proj.	E	Spin	χ	Mult.
0.0	1.0	0.047	\bar{M}	2.35	$\uparrow\uparrow$	+1	1
0.0	0.0	0.065	$\bar{\Gamma}$	-0.25	$\uparrow\uparrow$	+1	1
0.188	0.812	0.188	$\bar{X}\bar{M}$	1.85	$\uparrow\uparrow$	-1	4
0.322	0.322	0.331	$\bar{\Gamma}\bar{X}$	1.81	$\uparrow\downarrow$	+1	4
0.0	0.0	0.428	$\bar{\Gamma}$	-0.06	$\uparrow\uparrow$	-1	1
0.233	0.233	0.446	$\bar{\Gamma}\bar{X}$	1.39	$\uparrow\uparrow$	-1	4
0.0	0.0	0.480	$\bar{\Gamma}$	0.07	$\sim\uparrow\uparrow$	+2	1

D. Gosalbez-Martinez, I. Souza, D. Vanderbilt, PRB 92, 085138 (2015)

Breakdown of the Fermi surface of bcc iron

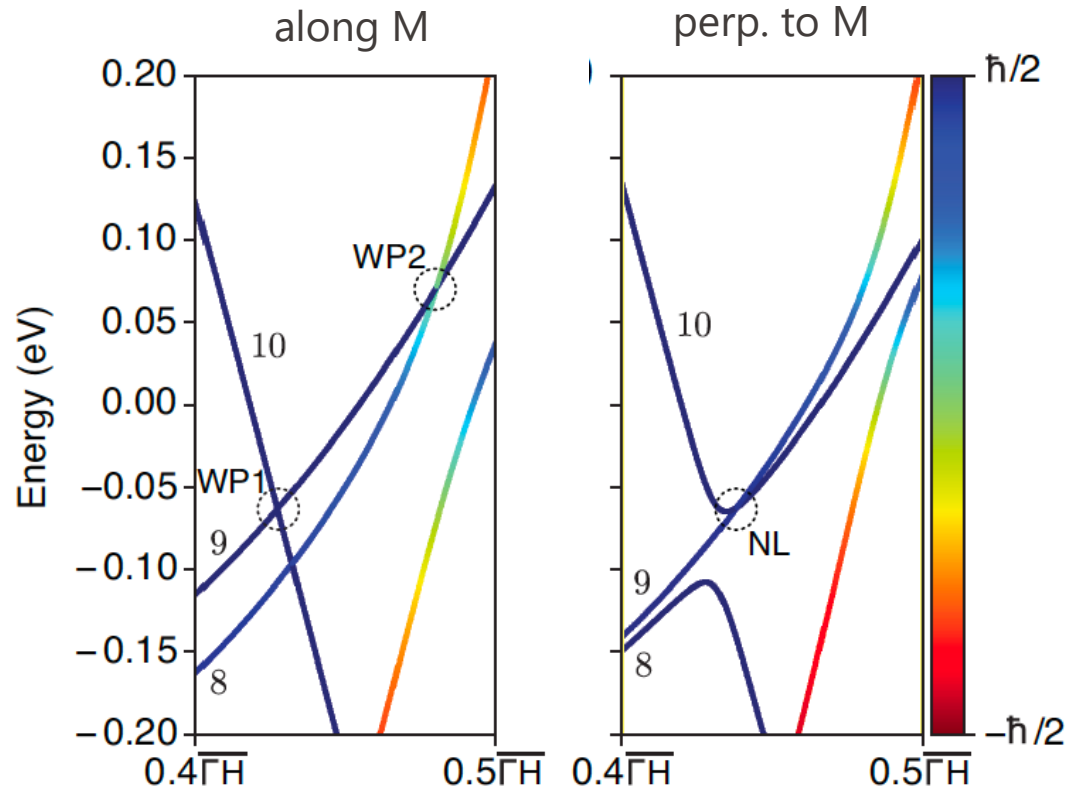


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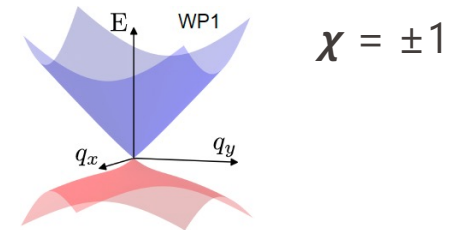
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D. Gosalbez-Martinez, I. Souza, D. Vanderbilt, PRB 92, 085138 (2015)
 D. Gosalbez-Martinez, G. Autés, O. V. Yazyev, PRB 102, 035419 (2020)

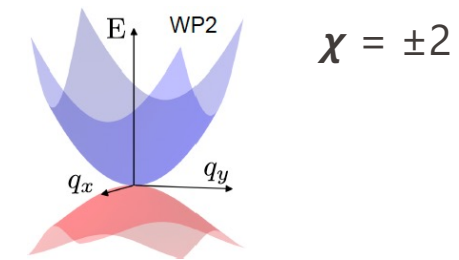
Breakdown of the Fermi surface of bcc iron



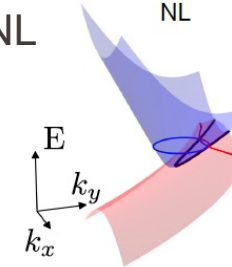
Elementary Weyl nodes WP1



Double Weyl nodes WP2



Nodal line NL



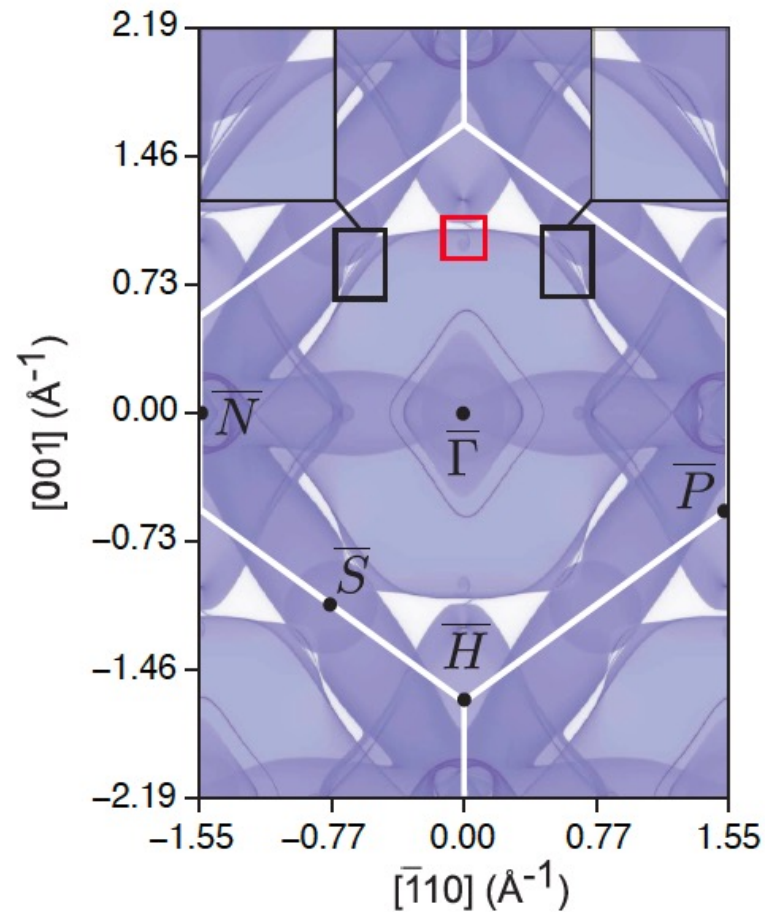
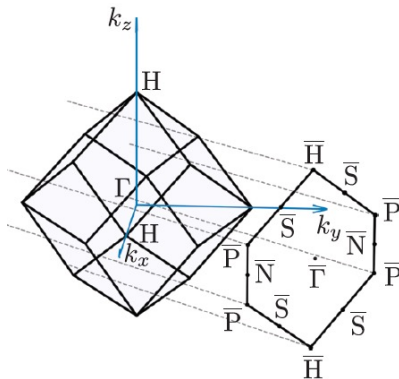
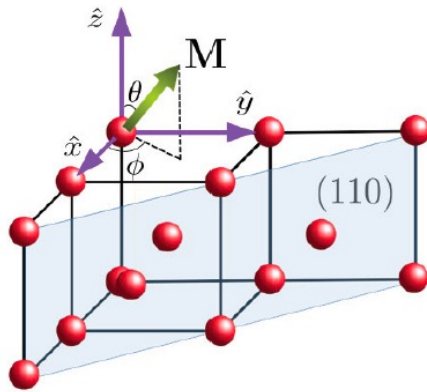
■ C3MP

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D. Gosalbez-Martinez, G. Autés, O. V. Yazyev, PRB 102, 035419 (2020)

Surface electronic structure of bcc iron

(110) surface
magnetization along [001]



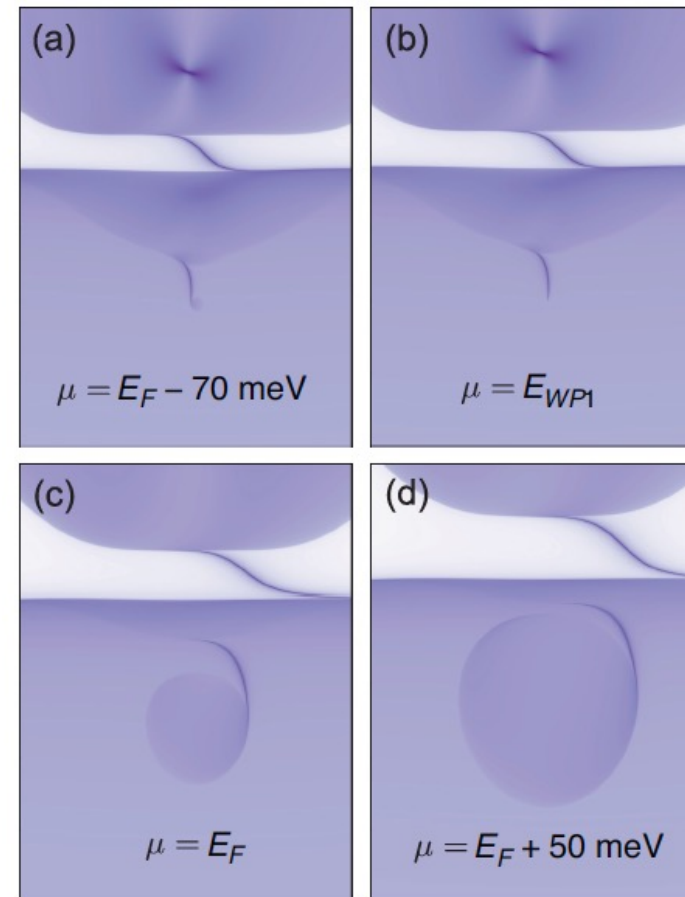
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D. Gosalbez-Martinez, G. Autés, O. V. Yazyev, PRB 102, 035419 (2020)

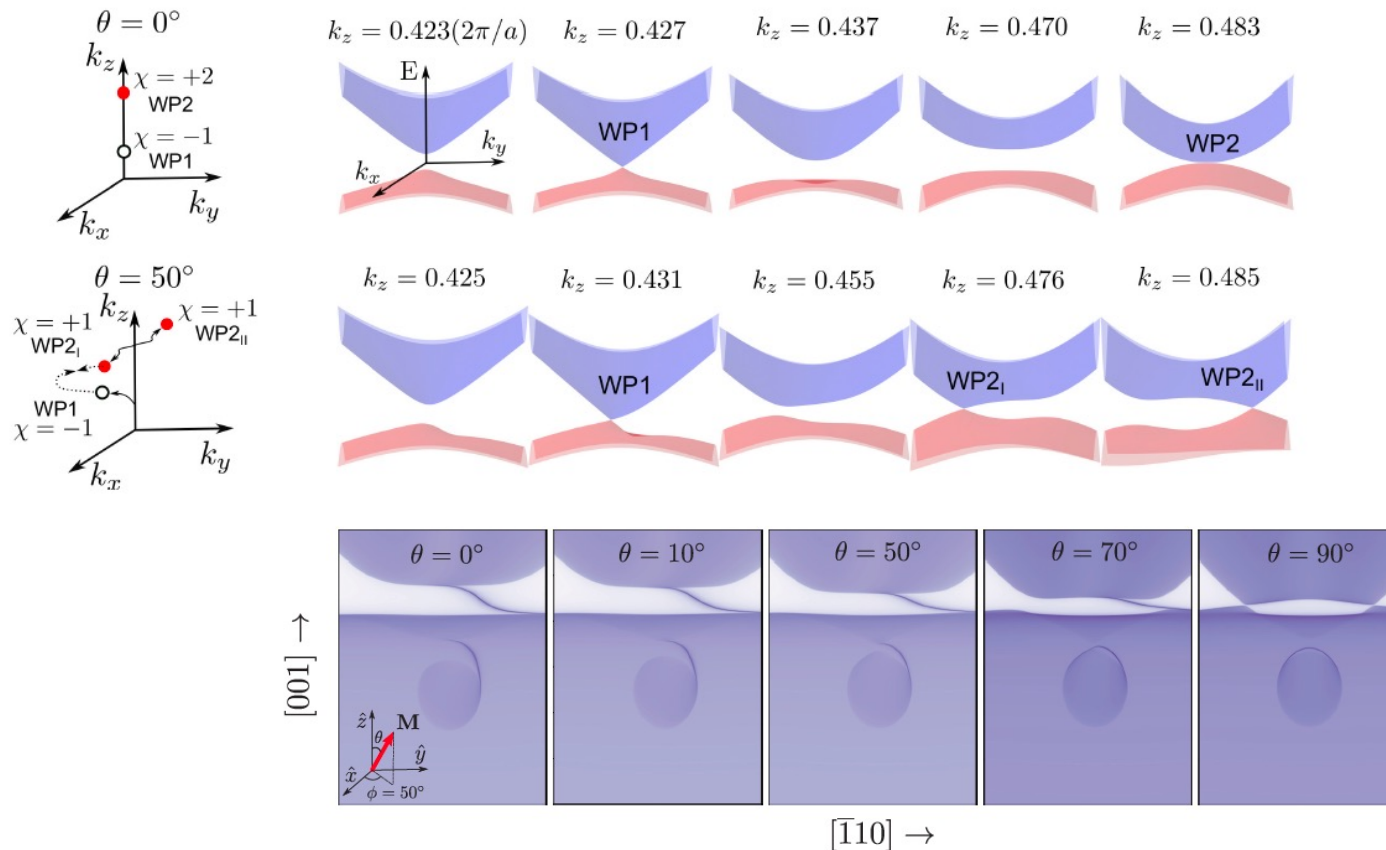
Surface electronic structure of bcc iron

- Close-up on the topological surface resonances



Topological phase transition

- Topological phase transition driven by tilting magnetization direction



Acknowledgments



Gabriel Autès
(Lausanne)



Quansheng Wu
(Lausanne)



Shengnan Zhang
(Lausanne)



Hyungjun Lee
(Lausanne)



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(Lausanne)

Theory: Hyungjun Lee, Yuting Qian (Lausanne),
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Nicola Marzari and his group (EPFL), Yi Liu (Beijing)

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Anna Isaeva (Dresden), Luca Moreschini, Eli Rotenberg, Aaron Bostwick, Jonathan Denlinger,
Alessandra Lanzara (Berkeley), Taisia Filatova, Alexey Kuznetsov (Moscow), Nan Xu, Ming Shi (PSI)

Funding

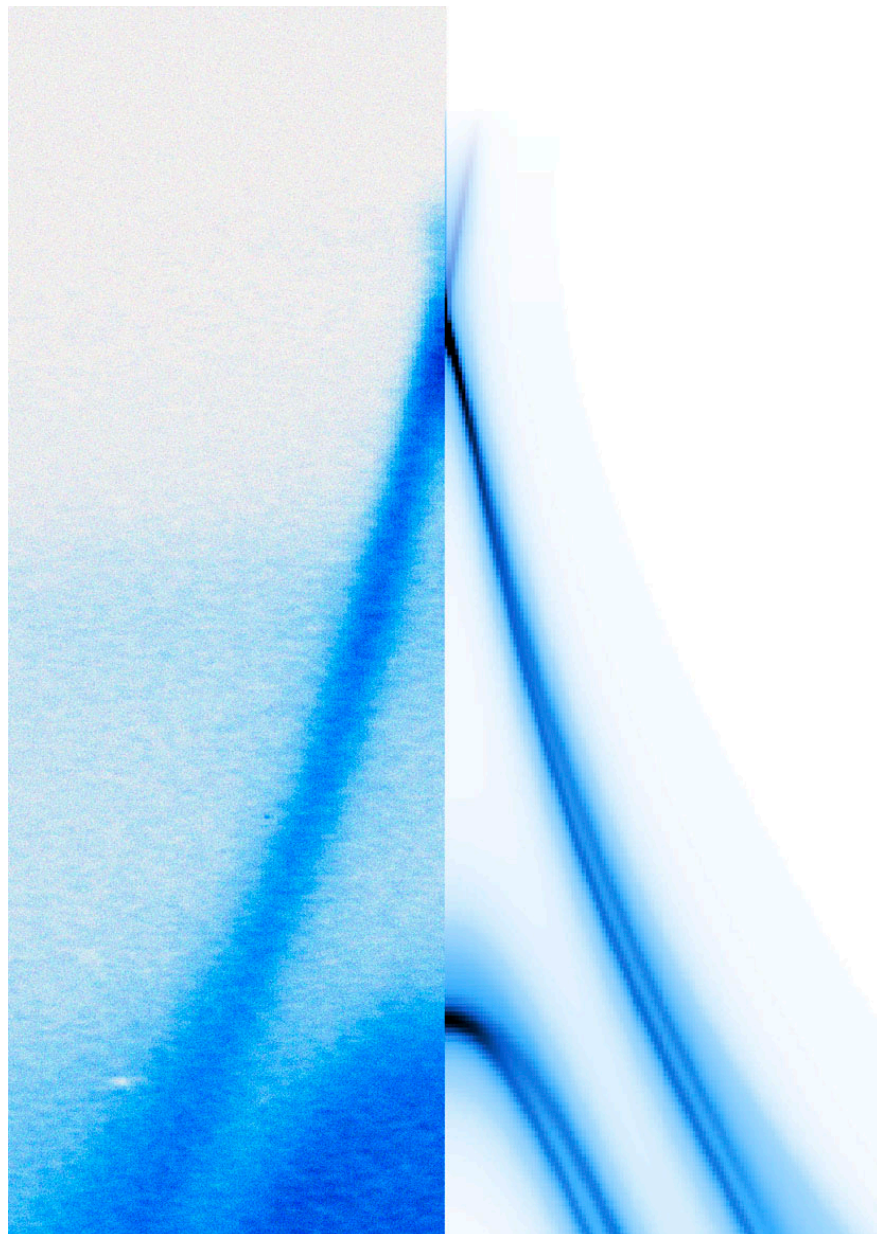
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Thank you